13. Volume and Surface Area

Exercise 13A

1. Question

Find the volume, the lateral surface area and the total surface area of the cuboid whose dimensions are:

- (i) length = 12 cm, breadth = 8 cm and height = 4.5 cm
- (ii) length = 26 m, breadth = 14 m and height = 6.5 m

(iii) length = 15 m, breadth = 6 m and height = 5 dm

(iv) length = 24 m, breadth = 25 cm and height = 6 m

Answer

(i) length = 12 cm, breadth = 8 cm and height = 4.5 cm

Volume of cuboid = (length × breadth × height) = $(12 \times 8 \times 4.5) = 432 \text{ cm}^3$

Lateral surface area of cuboid = $2(\text{length} + \text{breadth}) \times \text{height} = 2(12 + 8) \times 4.5 = 180 \text{ cm}^2$

Total surface area of cuboid = $2(\text{length} \times \text{breadth} + \text{breadth} \times \text{height} + \text{height} \times \text{length})$

$$= 2(12 \times 8 + 8 \times 4.5 + 4.5 \times 12) = 2(96 + 36 + 54) = 2 \times 186 = 372 \text{ cm}^2$$

(ii) length = 26 m, breadth = 14 m and height = 6.5 m

Volume of cuboid = (length × breadth × height) = $(26 \times 14 \times 6.5) = 2366 \text{ m}^3$

Lateral surface area of cuboid = 2(length + breadth) × height = $2(26 + 14) \times 6.5 = 520 \text{ m}^2$

Total surface area of cuboid = 2(length × breadth + breadth × height + height × length)

 $= 2(26 \times 14 + 14 \times 6.5 + 6.5 \times 26) = 2 \times 624 = 1248 \text{ m}^2$

(iii) length = 15 m, breadth = 6 m and height = 5 dm = (0.5 m)

Volume of cuboid = (length × breadth × height) = $(15 \times 6 \times 0.5) = 45 \text{ m}^3$

Lateral surface area of cuboid = 2(length + breadth) × height = $2(15 + 6) \times 0.5 = 21 \text{ m}^2$

Total surface area of cuboid = $2(\text{length} \times \text{breadth} + \text{breadth} \times \text{height} + \text{height} \times \text{length})$

 $= 2(15 \times 6 + 6 \times 0.5 + 0.5 \times 15) = 2(90 + 3.0 + 7.5) = 2 \times 100.5 = 201 \text{ m}^2$

(iv) length = 24 m, breadth = 25 cm and height = 6 m

Volume of cuboid = (length × breadth × height) = $(24 \times 0.25 \times 6) = 36 \text{ m}^3$

Lateral surface area of cuboid = 2(length + breadth) × height = $2(24 + 0.25) \times 6 = 291 \text{ m}^2$

Total surface area of cuboid = $2(\text{length} \times \text{breadth} + \text{breadth} \times \text{height} + \text{height} \times \text{length})$

 $= 2(24 \times 0.25 + 0.25 \times 6 + 6 \times 24) = 303 \text{ m}^2$

2. Question

Find the capacity of a closed rectangular cistern whose length is 8 m, breadth 6 m and depth 2.5 m. Also, find the area of the iron sheet required to make the cistern.

Answer

Given,

Dimensions of closed rectangular cistern = $8m \times 6m \times 2.5 m$

 \therefore Capacity of tank = volume of tank = (I × b × h) = 8 × 6 × 2.5 = 120 m³

Area of iron sheet required to make the tank = $2(lb + bh + hl) = 2(8 \times 6 + 6 \times 2.5 + 2.5 \times 8) = 2(48 + 15 + 20) = 2 \times 83 = 166m^2$

3. Question

The dimensions of a room are $(9 \text{ m} \times 8 \text{ m} \times 6.5 \text{ m})$. It has one door of dimensions $(2 \text{ m} \times 1.5 \text{ m})$ and two windows, each of dimensions $(1.5 \text{ m} \times 1 \text{ m})$. Find the cost of white washing the walls at Rs. 6.40 per square metre.

Answer

Given,

Dimensions of room = $9m \times 8m \times 6.5m$

Area of 4 walls = 2 (length + breadth) × height = 2 (9 + 8) × 6.5 = $13 \times 17 = 221 \text{ m}^2$

Dimensions of one door = $2m \times 1.5m$

Area of door = length × breadth = 2 × 1.5 = 3.0 m²

Dimensions of windows = $1.5m \times 1m$

Area of 2 windows = 2 ($I \times b$) = 2 (1.5×1) = 3.0 m²

Hence,

Area required for white-washing = Area of 4 walls - (area of door + area of 2 windows)

$$= 221 - (3 + 3) = 221 - 6 = 215 \text{ m}^2$$

 \therefore cost of white-washing 1 m² area = Rs. 6.40

 \therefore cost of white-washing 215 m² = 6.40 × 215 = Rs. 1376.

4. Question

How many planks of dimensions ($5m \times 25cm \times 10cm$) can be stored in a pit which is 20 m long, 6 m wide and 80 cm deep?

Answer

Given,

Dimensions of plank;

I = 5m

b = 25cm = 0.25 m

h = 10cm = 0.10 m

Dimensions of pit;

l = 20m

b = 6m

h = 80m

number of planks = $\frac{volume \ of \ pit}{volume \ of \ plank} = \frac{20 \times 6 \times 0.80}{5 \times 0.25 \times 0.10} = 768$

5. Question

How many bricks will be required to construct a wall 8 m long, 6 m high and 22.5 cm thick if each brick measures (25 cm \times 11.25 cm \times 6 cm)?

Answer

Given,

Dimensions of wall = $8m \times 6m \times 22.5 \text{ cm} = 800 \text{ cm} \times 600 \text{ cm} \times 22.5 \text{ cm}$

Dimensions of each brick = $25 \text{ cm} \times 11.25 \text{ cm} \times 6 \text{ cm}$

Hence,

Number of bricks required = $\frac{volume \ of \ wall}{volume \ of \ one \ brick} = \frac{800 \times 600 \times 22.5}{25 \times 11.25 \times 6} = 6400 \ bricks.$

6. Question

A wall 15 m long, 30 cm wide and 4 m high is made of bricks, each measuring

 $(22 \text{ cm} \times 12.5 \text{ cm} \times 7.5 \text{ cm})$. If $\frac{1}{12}$ of the total volume of the wall consists of mortar, how many bricks are there in the wall?

Answer

Given,

Dimensions of wall = $15m \times 30cm \times 4m = 1500 cm \times 30 cm \times 400 cm$

Dimensions of each brick = $22 \text{ cm} \times 12.5 \text{ cm} \times 7.5 \text{ cm}$

Volume of wall = $l \times b \times h = 1500 \times 30 \times 400 = 180000000 \text{ cm}^3$

Area of mortar = $1/12 \times \text{volume of wall} = \frac{1}{12} \times 180000000 = 15000000 \text{ cm}^3$

Hence,

Area occupied by bricks only = $180000000 - 15000000 = 165000000 \text{ cm}^3$

Number of bricks required = $\frac{volume \ for \ bricks \ only}{volume \ of \ one \ brick} = \frac{165000000}{22 \times 12.5 \times 7.5} = 8000 \ bricks.$

7. Question

An open rectangular cistern when measured from outside is 1.35 m long, 1.08 m broad and 90 cm deep. It is made up of iron, which is 2.5 cm thick. Find the capacity of the cistern and the volume of the iron used.

Answer

Given,

External Dimensions of cistern = $1.35m \times 1.08m \times 90cm = 135cm \times 108cm \times 90cm$

External volume of cistern = $1 \times b \times h = 135 \times 108 \times 90 = 1312200$ cm³

Internal dimensions of cistern = length = $135 - (2.5 \times 2) = 130$ cm

Breadth = $108 - (2.5 \times 2) = 103$ cm

Height = 90 - 2.5 = 87.5 cm

 \therefore internal volume of cistern = 130 \times 103 \times 87.5 = 1171625 cm³

Volumeof iron used = (External volume – Internal volume)

 $= 1312200 - 1171625 = 140575 \text{ cm}^3$

8. Question

A river 2 m deep and 45 m wide is flowing at the rate of 3 km per hour. Find the volume of water that runs into the sea per minute.

Answer

Given,

Depth of river (h) = 2 m

Breadth of river (b) = 45 m

Rate of flowing = 3 km/h

 $\therefore \text{ Length} = \frac{3000}{60} \text{ meter/min.}$

Volume of water = $1 \times b \times h = \frac{3000}{60} \times 2 \times 45 = 90 \times 50 = 4500 \text{ m}^3$

9. Question

A box made of sheet metal costs Rs 1620 at Rs 30 per square metre. If the box is 5 m long and 3 m wide, find its height.

Answer

Given,

Total cost of box made of sheet metal = Rs. 1620

Cost of per square meter metal = Rs. 30

: Area of box = $\frac{1620}{30}$ = 54 m²

Dimensions of box = $5m \times 3m \times height$

Let height of box = h meter

Total surface area of sheet = 2 (lb + bh + hl)

 $= 54 = 2 (5 \times 3 + 3h + 5h)$

= 8h = 27 - 15 = 12

$$= h = \frac{12}{9} = 1.5 m$$

Height of box = 1.5 meter.

10. Question

Find the length of the longest pole that can be put in a room of dimensions $(10 \text{ m} \times 10 \text{ m} \times 5 \text{ m})$.

2.01

Answer

Given,

Dimensions of room = $10m \times 10m \times 5m$

 \therefore length of longest pole can be put in room = diagonal of room

 $=\sqrt{l^2 + b^2 + h^2} = \sqrt{10^2 + 10^2 + 5^2} = \sqrt{225} = 15 m$

11. Question

How many person can be accommodated in a dining hall of dimensions $(20 \text{ m} \times 16 \text{ m} \times 4.5 \text{ m})$, assuming that each person requires 5 cubic metres of air?

Answer

Given,

Dimensions of dining hall = $20m \times 16m \times 4.5m$

Volume of hall = $20 \times 16 \times 4.5 = 1440 \text{ m}^3$

Volume of air required by one person = 5 m^3

· Number of persons in hall -	volume of hall	_ 1440 _ ,	288 norcone
	volume of air required by one person		200 per sons.

12. Question

A classroom is 10 m long, 6.4 m wide and 5 m high. If each student be given 1.6 m^2 of the floor area, how many students can be accommodated in the room? How many cubic metres of air would each student get?

Answer

Given,

Dimensions of classroom = $10m \times 6.4m \times 5m$

Area of room = length × breadth = $10 \times 6.4 = 64 \text{ m}^2$

Area of floor required by one student = 1.6 m^2

: Number of students can sit in classroom = $\frac{Area \ of \ floor}{area \ required \ by \ one \ student} = \frac{64}{1.6} = 40 \ students.$

Volume of classroom = $10 \times 6.4 \times 5 \text{ m}^3$

Air required by each student = $\frac{volume \ of \ room}{number \ of \ students} = \frac{10 \times 6.4 \times 5}{40}$

13. Question

The volume of a cuboid is $_{1536}$ m³. Its length is 16 m, and its breadth and height are in the ratio 3:2. Find the breadth and height of the cuboid.

Answer

Given,

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Volume of cuboid = 1536 \text{ m}^3
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Length of cuboid = 16 m

Ratio of breadth and height = 3:2

Let breadth = 3x

Let breadth = 2x

 \therefore Volume of cuboid = I × b × h

 $= 1536 = 16 \times 3x \times 2x$

$$= 6x^{2} = \frac{1536}{16} = 96$$
$$= x^{2} = \frac{96}{6} = 16$$
$$= x = \sqrt{16} = 4$$

Hence,

Breadth of cuboid = $3x = 3 \times 4 = 12m$

Height of cuboid = $2x = 2 \times 4 = 8m$

14. Question

The surface area of a cuboid is 758 cm^2 . Its length and breadth are 14 cm and 11 cm respectively. Find its height.

Answer

Given,

Surface area of cuboid = 758 cm^2

Length of cuboid = 14 cm

Breadth of cuboid = 11 cm

Let height of cuboid = h cm

Total surface area of cuboid = 2(lb + bh + hl)

 $= 758 = 2 (14 \times 11 + 11h + 14h)$

$$= 154 + 25h = \frac{758}{2} = 379$$

= 25h = 379 - 154 = 225

$$= h = \frac{225}{25} = 9$$

Height of cuboid = 9 meter.

15. Question

Find the volume, the lateral surface area, the total surface area and the diagonal of a cube, each of whose edges measures (a) 9m, (b) 6.5 cm. [Take $\sqrt{3} = 1.73$.]

Answer

Given,

a) Edge of cube (a) = 9m

Volume of cube = $a^3 = 9^3 = 729 \text{ m}^3$

Lateral surface area of cube = $4a^2 = 4 \times 9^2 = 4 \times 81 = 324 \text{ m}^2$

Total surface area of cube = $6a^2 = 6 \times 9^2 = 6 \times 81 = 486 \text{ m}^2$

Diagonal of cube = $\sqrt{3}$ a = $\sqrt{3} \times 9 = 1.73 \times 9 = 15.57$ m

b) Edge of cube (a) = 6.5 cm

Volume of cube = $a^3 = 6.5^3 = 274.625$ cm³

Lateral surface area of cube = $4a^2 = 4 \times 6.5^2 = 4 \times 42.25 = 169 \text{ cm}^2$

Total surface area of cube = $6a^2 = 6 \times 6.5^2 = 6 \times 42.25 = 253.5 \text{ cm}^2$

Diagonal of cube = $\sqrt{3}$ a = $\sqrt{3} \times 6.5 = 1.73 \times 6.5 = 11.245$ cm

16. Question

The total surface area of a cube is 1176 cm². Find its volume.

Answer

Given,

Total surface area of cube = 1176 cm^2

Let edge of cube = a cm

 $= 6 a^2 = 1176$

$$=a^2=\frac{1176}{6}=196$$

 \therefore Volume of cube = $a^3 = 14^3 = 2744$ cm³

17. Question

The lateral surface area of a cube is 900 cm². Find its volume.

Answer

Given,

Lateral surface area of cube = 900 cm^2

Let edge of cube = a cm

 $4a^2 = 900$

$$= a^2 = \frac{900}{4} = 225$$

 $= a = \sqrt{225} = 15 \ cm$

Volume of cube = $a^3 = 15^3 = 3375 \text{ cm}^3$

18. Question

The volume of a cube is 512 cm^3 . Find its surface area.

Answer

Given

Volume of cube = 512 cm^3

Let edge of cube = a cm

 $= a^3 = 512$ = a = $\sqrt[3]{512} = 8 \text{ cm}$

Total surface area of cube = $6 a^2 = 6 \times 8 \times 8 = 384 \text{ cm}^2$

19. Question

Three cubes of metal with edges 3 cm, 4 cm and 5 cm respectively are melted to form a single cube. Find the lateral surface area of the new cube formed.

Answer

Given,

Edge of three cubes $a_1 = 3 \text{ cm}$, $a_2 = 4 \text{ cm}$, $a_3 = 5 \text{ cm}$

Let edge of single cube formed = A cm

Sum of volume of three cubes = volume of single cube formed

$$= a_1^3 + a_2^3 + a_3^3 = A^3$$

 $= 3^3 + 4^3 + 5^3 = A^3$

 $A^3 = 27 + 64 + 125 = 216$

 $A = \sqrt[3]{216} = 6 \ cm$

Lateral surface area of new cube = $4a^2 = 4 \times 6 \times 6 = 144$ cm²

20. Question

In a shower, 5 cm of rain falls. Find the volume of water that falls on 2 hectares of ground.

Answer

Given,

Area of field = 2 hectare = 20000 m^2

Height of rainfall = 5 cm = 0.05 m

Volume of water that falls = Area \times height

 $= 20000 \times 0.05 = 1000 \text{ m}^3$

Exercise 13B

1. Question

Find the volume and curved surface area of a right circular cylinder of height 21 cm and base radius 5 cm.

Answer

So,

Given,

Height of cylinder = 21 cm

Radius of base = 5 cm

: volume of right circular cylinder = $\pi r^2 h = \frac{22}{7} \times 5 \times 5 \times 21 = 1650 \text{ cm}^3$

Curved surface area = $2\pi rh = 2 \times \frac{22}{7} \times 5 \times 21 = 660 \text{ cm}^2$

2. Question

The diameter of a cylinder is 28 cm and its height is 40 cm. Find the curved surface area, total surface area and the volume of the cylinder.

Answer

Given,

Diameter of cylinder = 28 cm Height of cylinder = 40 cm Radius of cylinder = $\frac{diameter}{2} = \frac{28}{2} = 14 \text{ cm}$ \therefore Curved surface area of cylinder = $2\pi rh = 2 \times \frac{22}{7} \times 14 \times 40 = 44 \times 40 \times 2 = 3520 \text{ cm}^2$ \therefore total surface area of cylinder = $2\pi rh + 2\pi r^2 = 2\pi r(h + r) = 2 \times \frac{22}{7} \times 14 \times 54 = 88 \times 54 = 4752 \text{ cm}^2$

 $\therefore \text{ Volume of cylinder} = \pi r^2 h = \frac{22}{7} \times 14 \times 14 \times 40 = 24640 \text{ cm}^3$

3. Question

Find the weight of a solid cylinder of radius 10.5 cm and height 60 cm if the material of the cylinder weigh 5 g per cm³.

Answer

Given,

Radius of cylinder = 10.5 cm

Height of cylinder = 60 cm

: Volume of cylinder =
$$\pi r^2 h = \frac{22}{7} \times 10.5 \times 10.5 \times 60 = 20790 \text{ cm}^3$$

 \therefore Weight of cylinder = volume of cylinder \times wt. of cylinder per gram

= 20790 × 5 g = 103950 g = 103.95 kg

4. Question

The curved surface area of a cylinder is $_{1210 \text{ cm}^2}$ and its diameter is 20 cm. Find its height and volume.

Answer

Given,

Curved surface area of cylinder = 1210 cm^2

Diameter of cylinder = 20 cm

Radius of cylinder = $\frac{20}{2}$ = 10 cm

Let height of cylinder = h cm

Curved surface area = $2\pi rh$

= 2nrh = 1210

$$= 2 \times \frac{22}{7} \times 10 \times h = 1210$$

$$= h = \frac{1210 \times 7}{44 \times 10} = 19.25 \text{ cm}$$

:. Volume of cylinder = $\pi r^2 h = \frac{22}{7} \times 10 \times 10 \times 19.25 = 6050 \text{ cm}^3$

5. Question

The curved surface area of a cylinder is 4400 cm² and the circumference of its base is 110 cm. Find the height and the volume of the cylinder.

Answer

Given,

Curved surface area of cylinder = 4400 cm^2

Circumference of its base = 110 cm

2nr = 110

$$= r = \frac{110}{2\pi} = \frac{110 \times 7}{44} = \frac{35}{2}cm$$

Let height of cylinder = h cm

C.S.A = 4400

2nrh = 4400

$$= 2 \times \frac{22}{7} \times \frac{35}{2} \times h = 4400$$
$$= h = \frac{4400 \times 7 \times 2}{44 \times 35} = 40 \ cm$$

: Volume of cylinder = $\pi r^2 h = \frac{22}{7} \times \frac{35}{2} \times \frac{35}{2} \times 40 = 110 \times 350 = 38500 \ cm^3$

6. Question

The radius of the base and the height of a cylinder are in the ratio 2:3. If its volume is $_{1617}$ cm³, find the total surface area of the cylinder.

Answer

Given,

Volume of cylinder = 1617 cm^3

Ratio of radius of base and height = 2:3

Let base radius = 2x cm

Let height = 3x cm

Volume = $\pi r^2 h$

$$=\frac{22}{7} \times 4x^2 \times 3x = 1617$$

$$= x^3 = \frac{1617 \times 7}{7}$$

$$= x = \sqrt[3]{42.875} = 3.5 \ cm$$

Hence,

Radius of cylinder = $2 \times 3.5 = 7$ cm

Height of cylinder = $3 \times 3.5 = 10.5$ cm

Total surface area of cylinder = $2\pi rh + 2\pi r^2 = 2\pi r (h + r) = 2 \times \frac{22}{7} \times 7 \times 17.5 = 770 \text{ cm}^2$

7. Question

The total surface area of a cylinder is 462 cm². Its curved surface area is one-third of its total surface area. Find the volume of the cylinder.

2.00

Answer

Given,

Total surface area of cylinder = 462 cm^2

 $2\pi rh = \frac{1}{3} \times 462 = 154$

Putting value of rh in equation (i)

$$\Rightarrow r^{2} + \frac{49}{2} = \frac{147}{2}$$
$$\Rightarrow r^{2} = \frac{147}{2} - \frac{49}{2} = \frac{98}{2} = 49$$
$$\Rightarrow r = \sqrt{49} = 7 \ cm$$

From (ii)

$$\Rightarrow rh = \frac{49}{2}$$
$$\Rightarrow h = \frac{49}{2 \times 7} = \frac{7}{2} cm$$

: Volume of cylinder = $\pi r^2 h = \frac{22}{7} \times 7 \times 7 \times \frac{7}{2} = 532 \text{ cm}^3$

8. Question

The total surface area of a solid is $_{231}$ cm² and its curved surface area is $\frac{2}{3}$ of the total surface area. Find the volume of the cylinder.

Answer

Total surface area of solid = 231 cm^2 $2\pi r(h + r) = 231$

 $\Rightarrow r (r + h) = \frac{(231 \times 7)}{44}$

$$\Rightarrow r^2 + rh = \frac{231 \times 7}{44} \dots \dots \dots \dots \dots \dots \dots \dots (i)$$

$$CSA = \frac{2}{3}TSA \ given$$

 $2\pi rh = \frac{2}{3} \times 231$

$$\Rightarrow \mathsf{rh} = \frac{2 \times 231 \times 7}{2 \times 3 \times 22} = \frac{49}{2} \dots \dots \dots \dots \dots \dots \dots \dots (ii)$$

Putting value of rh in (i) we get,

$$\Rightarrow r^{2} + \frac{49}{2} = \frac{231 \times 7}{44}$$
$$\Rightarrow r^{2} = \frac{1617}{44} - \frac{49}{2} = \frac{1617 - 1078}{44} = \frac{539}{44} = 12.25$$

 \Rightarrow r = $\sqrt{12.25}$ = 3.5 cm

From equation (ii)

$$\Rightarrow rh = \frac{49}{2}$$
$$\Rightarrow h = \left(\frac{49}{3.5 \times 2}\right) = 7 \ cm$$

 $\therefore \text{ Volume of cylinder} = \pi r^2 h = \frac{22}{7} \times 3.5 \times 3.5 \times 7 = 269.5 \text{ cm}^3$

9. Question

The sum of the height and radius of the base of a solid cylinder is 37 m. If the total surface area of the cylinder be $_{1628}$ m², find its volume.

Answer

Given,
Total surface area of cylinder = 1628 m²
Sum of height and radius = (h + r) = 37 m

$$2nr (h + r) = 1628$$

 $2nr \times 37 = 1628$
 $\Rightarrow r = \frac{1628 \times 7}{2 \times 22 \times 37} = 7 m$
 $\therefore r + h = 37$
 $\Rightarrow h = 37 - 7 = 30 m$
 \therefore Volume of cylinder = $nr^{2}h = \frac{22}{7} \times 7 \times 7 \times 30 = 4620 m^{3}$
10. Question

The ratio between the curved surface area and the total surface area of a right circular cylinder is 1:2. Find the volume of the cylinder if its total surface area is $_{616}$ cm².

Answer

Given,

Total surface area of cylinder = 616 cm^2

$$\Rightarrow \frac{C.S.A}{T.S.A} = \frac{1}{2}$$
$$\Rightarrow \frac{2\pi rh}{\{2\pi r(h+r)\}} = \frac{1}{2}$$
$$\Rightarrow \frac{h}{h+r} = \frac{1}{2}$$
$$\Rightarrow 2h = r + h$$

 \Rightarrow h = r....(i) $2\pi r (h + r) = 616$ \Rightarrow r (r + r) = $\frac{616 \times 7}{44}$ = 198 $\Rightarrow r^2 = \frac{198}{2} = 49$ \Rightarrow r = $\sqrt{49}$ = 7 cm H = 7 cm $\therefore \text{ Volume of cylinder} = \pi r^2 h = \frac{22}{7} \times 7 \times 7 \times 7 = 22 \times 49 = 1078 \text{ cm}^3$

11. Question

 1 cm^3 of gold is drawn into a wire 0.1 mm in diameter. Find the length of the wire.

Answer

Given, Diameter of wire = 0.1 mm = 0.01 cmRadius of wire = $\frac{0.01}{2}$ cm Volume of gold = 1 cm^3 $\Rightarrow \pi r^2 h = 1$ $\Rightarrow \frac{22}{7} \times \left(\frac{0.01}{2}\right)^2 \times h = 1$ \Rightarrow h = $\frac{200 \times 200 \times 7}{22 \times 1 \times 1}$ = 12727.27 cm or 127.27 m Length of wire = 127.27 meter.

12. Question

The radii of two cylinders are in the ratio 2:3 and their heights are in the ratio 5:3. Calculate the ratio of their volumes and the ratio of their curved surfaces.

Answer

Given,

Ratio of radii of two cylinders = R_1 : R_2 = 2 : 3

Ratio of their heights = H_1 : H_2 = 5 : 3

: Ratio of volumes of cylinders = $\frac{V_1}{V_2} = \frac{\pi R_1^2 H_1}{\pi R_2^2 H_2} = \frac{4 \times 5}{9 \times 3} = \frac{20}{27} OR \ 20 : 27.$

 $\therefore \text{ Ratio of their curved surface area} = \frac{A_1}{A_2} = \frac{2\pi R_1 H_1}{2\pi R_2 H_2} = \frac{2\times 5}{3\times 3} = \frac{10}{9} \text{ or } 10:9.$

13. Question

A powder tin has a square base with side 12 cm and height 17.5 cm. another is cylindrical with diameter of its base 12 cm and height 17.5 cm. Which has more capacity and by how much?

Answer

Given,

Side of square base = 12 cm

Height = 17.5 cm

Volume of tin = $lbh = 12 \times 12 \times 17.5 = 2520 \text{ cm}^3$

Diameter of cylindrical base = 12 cm

Radius = $\frac{12}{2} = 6 \ cm$

Height of cylinder = 17.5 cm

Volume of tin in cylinder = $\pi r^2 h = \frac{22}{7} \times 6 \times 6 \times 17.5 = \frac{13860}{7} = 1980 \text{ cm}^3$

Hence,

Capacity of square tin is more by = $2520 - 1980 = 540 \text{ cm}^3$

14. Question

A cylindrical bucket, 28 cm in diameter and 72 cm high, is full of water. The water is emptied into a rectangular tank, 66 cm long and 28 cm wide. Find the height of the water level in the tank.

Answer

Given,

Diameter of cylindrical bucket = 28 cm

Radius of bucket = $\frac{28}{2} = 14$ cm

Height of bucket = 72 cm

Volume of water in bucket = $\pi r^2 h = \frac{22}{7} \times 14 \times 14 \times 72 \ cm^3$

Length of rectangular tank = 66 cm

Width of tank = 28 cm

Let rise in water level in rectangular tank = h cm

: Volume of cylinder = Volume of rectangular tank

$$\Rightarrow \frac{22}{7} \times 14 \times 14 \times 72 = 66 \times 28 \times h$$

$$\Rightarrow h = \frac{22 \times 14 \times 14 \times 72}{7 \times 66 \times 28} = 24 \ cm.$$

15. Question

If 1 cm^3 of cast iron weighs 21 g, find the weight of a cast iron pipe of length 1 m with a bore of 3 cm in which the thickness of the metal is 1 cm.

Answer

Given,

Weight of 1 cm³ cast iron = 21 g

Length of wire = h = 1 m = 100 cm

Internal radius (r₁) = $\frac{3}{2} = 1.5$ cm

Thickness of metal = 1 cm

So, External radius $(r_2) = 1.5 + 1 = 2.5$ cm

Volume of metal = (External volume - internal volume)

$$= \pi r_2^2 h - \pi r_1^2 h = \pi h (r_2^2 - r_1^2) = \frac{22}{7} \times 100 (2.5 + 1.5) (2.5 - 1.5)$$

$$=\frac{22}{7} \times 100 \times 4 \times 1 \text{ cm}^3$$

Weight of metal = $\frac{22}{7} \times 100 \times 4 \times 1 \times 21 = 26400 \ gm = 26.4 \ kg$.

16. Question

A cylindrical tube, open at both ends, is made of metal. The internal diameter of the tube is 10.4 cm and its length is 25 cm. The thickness of the metal is 8 mm everywhere. Calculate the volume of the metal.

Answer

Given,

Internal diameter of tube = 10.4 cm

Internal radius of tube = $\frac{10.4}{2} = 5.2 \ cm$

Thickness of metal = 8 mm = 0.8 cm

External radius of tube = 5.2 + 0.8 = 6 cm

Length of tube = 25 cm

.. Volume of metal = (external volume – internal volume)

=
$$\pi h (6^2 - 5.2^2) = \frac{22}{7} \times 25 \times 11.2 \times 0.8 = 22 \times 32 = 704 \ cm^3$$

17. Question

The barrel of a fountain pen, cylindrical in shape, is 7 cm long and 5 mm in diameter. A full barrel of ink in the pen will be used up on writing 330 words on an average. How many words would use up a

bottle of ink containing one-fifth of a litre?

Answer

Given,

Length of cylindrical barrel (h) = 7 cm

Diameter = 5 mm

Radius = $\frac{5}{2}$ = 2.5 mm = 0.25 cm

Volume of cylindrical barrel = $\pi r^2 h = \frac{22}{7} \times 0.25 \times 0.25 \times 7 = \frac{5.5}{4} cm^3$

 $\therefore \frac{5.5}{4} \text{ cm}^3 \text{ volume of barrel is used for writing} = 330 \text{ words}$ $\therefore \frac{5.5}{4} \times 1000 \text{ cm}^3 \text{ will be used for writing} = 330 \times \frac{4}{5.5} \times \frac{1}{8} \times 1000 = 48000 \text{ words}$

18. Question

A lead pencil consists of a cylinder of wood with a solid cylinder of graphite fitted into it. The diameter of the pencil is 7 mm, the diameter of the graphite is 1 mm and the length of the pencil is 10 cm. calculate the weight of the whole pencil, if the specific gravity of the wood is 0.7 g/cm^3 and that of the graphite is 2.1 g/cm^3 .

Answer

Given,

Diameter of pencil = 7 mm

Radius of pencil =
$$\frac{7}{2}$$
 mm = $\frac{0.7}{2}$ cm

Diameter of graphite = 1 mm

Radius of graphite = $\frac{1}{2}mm = \frac{0.1}{2}cm$

Volume of graphite = $\pi r^2 h = \frac{22}{7} \times \frac{0.1}{2} \times \frac{0.1}{2} \times 10 = \frac{0.55}{7} cm^3$

Weight of graphite = volume × specific gravity of graphite

$$=\frac{0.55}{7} \times 2.1 = 0.165 g$$

Volume of wood = volume of pencil - volume of graphite

$$= \frac{22}{7} \times ((0.35)^2 - (0.05)^2) \times 10 \times 0.7$$
$$= \frac{22}{7} \times (0.1225 - 0.0025) \times 7 = 2.64 g$$

 \therefore Total weight of the pencil = weight of wood + weight of graphite

$$= 0.165 + 2.64 = 2.805 g.$$

Exercise 13C

1. Question

Find the volume, curved surface area and the total surface area of a cone having base radius 35 cm and height 84 cm.

Answer

Given,

Radius of the cone = 35cm

Height of the cone = 84cm

Curved surface area = πrl

So, we need to find out the I;

I = slant height

 $l = \sqrt{h^2 + r^2}$ $l = \sqrt{84^2 + 35^2} = \sqrt{7056 + 1225} = \sqrt{8281}$ | = 91cmCurved surface area = $\frac{22}{7} \times 35 \times 91$ $= 110 \times 91 = 10010$ cm² Volume of the cone = $\frac{1}{3}\pi r^2 h$ $=\frac{1}{3} \times \frac{22}{7} \times 35 \times 35 \times 84$ = 88 × 1225 $= 107800 \text{ cm}^2$ Total surface area = $\pi rl + \pi r^2$ $= 10010 + \frac{22}{7} \times 35 \times 35$ = 10010 + 3850 = 13860

Total surface area = 13860 cm²

2. Question

Find the volume, curved surface area and the total surface area of a cone whose height and slant height are 6 cm and 10 cm respectively. (Take $\pi = 3.14$)

Answer

Given,

Height (h) = 6cmSlant height (I) = 10cm $r = \sqrt{l^2 - h^2}$ $r = \sqrt{(10)^2 - (6)^2}$ $r = \sqrt{100 - 36} = \sqrt{64}$ r = 8cmVolume of the cone = $\frac{1}{3}\pi r^2 h$ $=\frac{1}{3}\times\frac{22}{7}\times8\times8\times6$ $=\frac{8448}{21}$ = 401.92cm² Curved surface area = πrl Curved surface area = $\frac{22}{7} \times 8 \times 10$ $=\frac{1760}{7}=251.2$ cm² Total surface area = $\pi r(r + I)$ $=\frac{22}{7} \times 8 \times (8 + 10)$ $=\frac{22}{7} \times 8 \times 18$ $=\frac{3168}{7}$ = 452.16 cm²

3. Question

The volume of a right circular cone is (100π) cm³ and its height is 12 cm. Find its slant height and its curved surface area.

Answer

Given,

h = 12 cm

Volume of the cone = 100π cm³

$$=\frac{1}{3}\pi r^2 h = 100\pi$$

 $r^{2}h = 100 \times 3$

$$r^{2} \times 12 = 100 \times 3$$

$$r^{2} = \frac{100 \times 3}{12} = 25$$

$$r = 5 \text{ cm}$$

$$l = \sqrt{h^{2} + r^{2}}$$

$$= \sqrt{(12)^{2} + (5)^{2}}$$

$$= \sqrt{144 + 25}$$

$$= \sqrt{169} = 13$$

Curved surface area = πrl

= п × 5 × 13

 $= (65\pi) \text{ cm}^2$

4. Question

The circumference of the base of a cone is 44 cm and its slant height is 25 cm. Find the volume and curved surface area of the cone.

Answer

Given,

Circumference of the base of the cone = 44cm

 $2\pi r = 44cm$

$$r = \frac{44 \times 7}{2 \times 22} = 7$$

r = 7cm

$$h = \sqrt{l^2 - r^2}$$

= $\sqrt{(25)^2 - (7)^2}$
= $\sqrt{625 - 49}$

$$=\sqrt{576}=24$$

 $volume = \frac{1}{3}\pi r^2 h$

$$=\frac{1}{3}\times\frac{22}{7}\times7\times7\times24$$

 $= 22 \times 56 = 1232$

Volume = 1232 cm^3

Curved surface area = πrl

$$=\frac{22}{7}\times7\times25$$

 $= 550 \text{ cm}^2$

5. Question

A cone of slant height 25 cm has a curved surface area 550 cm². Find the height and volume of the cone.

Answer

Given,

Curved surface area = 550 cm^2

nrl = 550 $\frac{22}{7} \times r \times 25 = 550$ $r = \frac{550 \times 7}{22 \times 25}$ r = 7cm $h = \sqrt{l^2 - h^2} = \sqrt{25^2 - 7^2}$ $=\sqrt{625-49}=\sqrt{576}=24$ h = 24cmVolume = $\frac{1}{3}\pi r^2 h$ $=\frac{1}{3}\times\frac{22}{7}\times7\times7\times24$ $= 24 \times 56$

Volume = 1232cm³

6. Question

Find the volume of a cone having radius of the base 35 cm and slant height 37 cm.

Answer

Given,

r = 35cm

I = 37 cm

Volume of the cone =
$$\frac{1}{3}\pi r^2 h$$

= $\frac{1}{3} \times \frac{22}{7} \times 38 \times 35 \times h$
= $\frac{3850}{3}h$
 $h = \sqrt{l^2 - h^2} = \sqrt{37^2 - 35^2}$
= $\sqrt{1369 - 1225}$
= $\sqrt{144} = 12$
 $volume = \frac{3850}{3} \times 12$

Volume = 1540 cm^3

7. Question

The curved surface area of a cone is 4070 cm² and its diameter is 70 cm. Find its slant height.

Answer

Given,

$$r = \frac{70}{2} = 35cm$$

Curved surface area = 4070

$$l = \frac{4070}{\pi r}$$

 $=\frac{4070 \times 7}{22 \times 35}$ $=\frac{814}{22} = 37 \text{ cm}$

8. Question

How many metres of cloth, 2.5 m wide, will be required to make a conical tent whose base radius is 7 m and height 24 metres?

Answer

Given,

Radius = 7cm

h = 24cm

$$l = \sqrt{h^2 + r^2}$$

= $\sqrt{(24)^2 + (7)^2}$
= $\sqrt{576 + 49}$
= $\sqrt{625}$
= 25m
Curved surface area of the tent = nrl

$$=\frac{22}{7} \times 7 \times 25$$

Length of cloth = $\frac{area}{width}$

$$=\frac{550}{2.5}=220m$$

9. Question

A right circular cone is 3.6 cm high and the radius of its base is 1.6 cm. It is melted and recast into a right circular cone having base radius 1.2 cm. Find its height.

Answer

When we melt any shape, and recast into another shape than volume of both shapes remain same.

Radius of the circular cone $(r_1) = 1.6$ cm

Height of the circular cone $(h_1) = 3.6$ cm

Radius of the new circular cone $(r_2) = 1.2$ cm

Let height of the new circular cone be h_2

Volume of the circular cone = volume of the new circular cone

$$\frac{1}{3}\pi r_1^2 h = \frac{1}{3}\pi r_2^2 h$$

 $(1.6)^2 \times (3.6) = (1.2)^2 \times h_2$

$$h_2 = \frac{(1.6)^2 \times 3.6}{(1.2)^2} = \frac{1.6 \times 1.6 \times 3.6}{1.2 \times 1.2} = 64$$

$$h_2 = 64 \text{ cm}$$

So, the height of the new circular cone will be 64cm

10. Question

Two cones have their heights in the ratio 1:3 and the radii of their bases in the ratio 3:1. Show that their volumes are in the ratio 3:1.

Answer

Given,

Ratio of the heights = h_1 : h_2 = 1:3

Let the heights of the cones be x and 3x,

Ratio of radius of base of the two cones = $r_1:r_2 = 3:1$

So,

Let the radius be 3x and x for the cones and volume will be v_1 and v_2

$\frac{v_1}{v_2} = \frac{\frac{1}{3}\pi r_1^2 h_2}{\frac{1}{3}\pi r_2^2 h_2}$	
$=\frac{(3x)^2 \times x}{x^2 \times 3x}$	
$=\frac{9x^2}{3x^2}$	
$\frac{v_1}{v_2} = \frac{3}{1}$	
So, ratio of th	e volume of the two cones will be 3:1

11. Question

A circus tent is cylindrical to a height of 3 meters and conical above it. If its diameter is 105 m and the slant height of the conical portion is 53 m, calculate the length of the canvas 5 m wide to make the required tent.

Answer

Given,

Cylindrical height of the tent = 3m

Diameter of the base of the cone = 105

Radius = $\frac{105}{2}$

Height of the conical portion = 53m

Area of canvas = curved surface area of conical part + curved surface area of cylindrical part

= nrl + 2nrh

 $=\frac{22}{7} \times \frac{105}{2} \times 53 + 2 \times \frac{22}{7} \times \frac{105}{2} \times 3$ = 8745 + 990 $= 9735m^{2}$ Length of canvas = area/width

$$=\frac{9735}{5}=1947m$$

Hence the length of the canvas will be 1947m

12. Question

A conical tent is to accommodate 11 persons. Each person must have 4 m² of the space on the ground and 20 m^3 of air to breath. Find the height of the cone.

Answer

Given, Number of person in the room = 11Each person covers area = $4m^2$ Total area covered by all = $44m^2$ $nr^2 = 44$ $r^2 = 44 \times \frac{7}{22} = 14$ Volume of the cone = $220m^3$ We know that, Volume of the cone = $\frac{1}{3}\pi r^2 h$ $\frac{1}{3}\pi r^2 h = 220$ $\frac{1}{3} \times \frac{22}{7} \times 14 \times h = 220$ $h = \frac{220 \times 3 \times 7}{22 \times 14} = 15m$

Hence, the height of the cone will be 15m

13. Question

A cylindrical bucket, 32 cm high and 18 cm of radius of the base, is filled with sand. This bucket is emptied on the ground and a conical heap of sand is formed. If the height of the conical heap is 24 cm, find the radius and the slant height of the heap.

Answer

Let the radius of the heap be r and the slant height h, So, we have Height of the cylindrical bucket = 32cm Radius of the base of cylindrical bucket = 18cm Height of the conical heap = 24cm Volume of cylinder = volume of cone $\pi r^2 h = \frac{1}{3}\pi r^2 h$ $r^2 = \frac{18 \times 18 \times 32 \times 3}{24}$ $r^2 = 18 \times 8 \times 4$ $r = 18 \times 2$ r = 36cmslant height I = $\sqrt{h^2 + r^2}$ $=\sqrt{(24)^2+(36)^2}$ $=\sqrt{576 + 1296}$ $=\sqrt{1872}$ I = 43.27cm

14. Question

A cylinder and a cone have equal radii of their bases and equal heights. If their curved surface areas are in the ratio 8:5, show that the radius and height of each has the ratio 3:4.

Answer

Given,

Curved surface area of cylinder = curved surface area of cone = 8:5

Let C.S.A of cylinder = 8x

C.S.A of cone = 5x

As mention above cone and cylinder have equal radius and equal height

$$\frac{CSA \ of \ cylinder}{CSA \ of \ cone} = \frac{8x}{5x}$$
$$\frac{2\pi rh}{\pi rl} = \frac{8}{5}$$
$$\frac{2h}{\sqrt{h^2 + r^2}} = \frac{8}{5}$$

 $\left(\frac{2h}{\sqrt{h^2 + r^2}}\right)^2 = \left(\frac{8}{5}\right)^2$ $\frac{4h^2}{h^2 + r^2} = \frac{64}{25}$ $100h^2 = 64h^2 + 64r^2$ $100h^2 - 64h^2 = 64r^2$ $36h^2 = 64r^2$ $\frac{r^2}{h^2} = \frac{36}{64}$ $\frac{r}{h} = \frac{6}{8}$ $\frac{r}{h} = \frac{3}{4}$

15. Question

An iron pillar consists of a cylindrical portion 2.8 m high and 20 cm in diameter and a cone 42 cm high is surmounting it. Find the weight of the pillar, given that 1 cm^3 of iron weighs 7.5 g

Answer

Given,

Height of cylinder R = 2.8m = 280cm

Radius = $\frac{20}{2} = 10cm$

Height of cone = 42cm

Volume of pillar = volume of cone + volume of cylinder

$$= \frac{1}{3}\pi r^{2}h + \pi r^{2}h$$

$$= \frac{1}{3} \times \frac{22}{7} \times 10 \times 10 \times 42 + \frac{22}{7} \times 10 \times 10 \times 280$$

$$= \frac{22}{7} \times 100[14 + 280]$$

$$= \frac{22}{7} \times 100 \times 294$$

$$= \frac{646800}{7} = 92400$$

Given that,
Weight of 1 cm³ iron = 7.5gm
Weight of the pillar = 92400 \times 75

Weight of the pillar = 693000g

= 693kg

16. Question

The height of a cone is 30 cm. A small cone is cut off at the top by a plane parallel to the base. If its volume be $\frac{1}{27}$ of the volume of the given cone, at what height above the base, the section has been made?

Answer

Let's suppose the smaller cone have the radius r and height h cm

And radius of the given cone be R cm

Height of the original cone = 30cm



 $n^{2} = 1000$

h = 10cm

Height of the small cone = 10cm

AC = OA-OC

AC = 30-10 = 20

Hence selection has been made at height of 20cm above the base.

17. Question

From a solid right circular cylinder with height 10 cm and radius of the base 6 cm, a right circular cone of the same height and base is removed. Find the volume of the remaining solid. (Take π = 3.14.)

Answer

Height of the cylinder = 10cm

Radius of the cylinder = 6cm

The height and base of the cone is equals to the height and base of the cylinder.

Volume of the remaining solid = volume of cylinder – volume of cone

$$= \pi r^2 h - \frac{1}{3}\pi r^2 h$$
$$= \frac{2}{3}\pi r^2 h$$
$$= \frac{2}{3} \times 3.14 \times 6 \times 6 \times 10$$

Volume of remaining solid = 753.6 cm³

18. Question

Water flows at the rate of 10 meters per minute through a cylindrical pipe 5 mm in diameter. How long would it take to fill a conical vessel whose diameter at the surface 40 cm and depth 24 cm?

Answer

Given,

Radius of the cylindrical pipe = $\frac{5}{2}$ = 2.5mm

= 0.25cm [as we know 10mm = 1cm]

Water flowing per minute through cylindrical pipe = $\pi (0.25)^2 \times 1000$

Radius of the conical vessel =
$$\frac{40}{2} = 20cm$$

Depth of the vessel = 24cm

Volume of the vessel = $\frac{1}{3}\pi(20)^2 \times 24$

Let the time to fill the conical vessel be x minute,

Water flowing per minute through cylindrical pipe x x = volume of conical vessel

$$X = \frac{\frac{1}{2}\pi(20)^2 \times 24}{\pi(0.25)^2 \times 1000}$$
$$X = \frac{20 \times 20 \times 8}{0.25 \times 0.25 \times 1000}$$

x = 51 min 12 sec.

Hence the required time to fill a conical vessel is 51min 12 sec

Exercise 13D

1. Question

Find the volume and surface area of a sphere whose radius is:

(i) 3.5 cm

(ii) 4.2 cm

(iii) 5 m

Answer

(i) Radius of sphere = 3.5cm Volume = $\frac{4}{2}\pi r^3$ $=\frac{4}{3} \times \frac{22}{7} \times 3.5 \times 3.5 \times 3.5$ $= 179.67 \text{ cm}^3$ Surface area = $4\pi r^2$ $= 4 \times \frac{22}{7} \times 3.5 \times 3.5$ $= 2 \times 22 \times 3.5 = 154 \text{ cm}^2$ (ii) R = 4.2 cmVolume = $\frac{4}{3}\pi r^3$ $=\frac{4}{2} \times \frac{22}{7} \times 4.2 \times 4.2 \times 4.2$ = 310.464 cm² Surface area = $4\pi r^2$ $= 4 \times \frac{22}{7} \times 4.2 \times 4.2$ $= 4 \times 22 \times .6 \times 4.2$ = 221.76 cm²

(iii) R = 5 cmVolume = $\frac{4}{2}\pi r^3$ $=\frac{4}{3}\times\frac{22}{7}\times5\times5\times5$ $=\frac{11000}{21}=523.80$ cm³ Surface area = $4\pi r^2$ $= 4 \times \frac{22}{7} \times 5 \times 5$ $=\frac{20 \times 110}{7} = 314.28 \text{ cm}^2 +$

2. Question

The volume of a sphere is 38808 cm³. Find its radius and hence its surface area.

Answer

Volume of sphere = 38808 cm³

 $\frac{4}{2}\pi r^3 = 38808$ $r^3 = \frac{38808 \times 3}{4\pi}$ $r^3 = \frac{38808 \times 3 \times 7}{4 \times 22}$ $r^3 = 441 \times 21$ $r^3 = 21 \times 21 \times 21$ r = 21cm surface area = $4\pi r^2$

$$= 4 \times \frac{22}{7} \times 21 \times 21$$

= 5544 cm³

3. Question

Find the surface area of a sphere whose volume is 606.375 m³.

Answer

Given,

 $Volume = 606.375 cm^3$

 $\frac{4}{2}\pi r^3 = 606.375$

$$r^{3} = \frac{606.375 \times 3}{4\pi}$$

$$r^{3} = \frac{606.375 \times 3 \times 7}{4 \times 21}$$

$$r^{3} = \frac{12733.875}{88}$$

$$r^{3} = 144.703$$

$$r = 5.25m$$
Surface area = $4\pi r^{2}$

$$= 4 \times \frac{22}{7} \times 5.25 \times 5.25$$

$$= 346.5m^{2}$$

4. Question

.ne. The surface area of a sphere is $_{394.24}$ m². Find its radius and volume.

Answer

Given,

Surface area = $394.24m^2$

 $4\pi r^2 = 394.24$

 $4 \times \frac{22}{7} \times r^2 = 394.24$

$$r^2 = \frac{394.24 \times 7}{22 \times 4}$$

 $r^2 = \frac{2759.68}{100}$

 $r^2 = 31.36$

Volume = $\frac{4}{3}\pi r^3$

$$=\frac{4}{3} \times \frac{22}{7} \times 5.6 \times 5.6 \times 5.6$$

$$=\frac{4}{2} \times 22 \times 0.8 \times 5.6 \times 5.6$$

= 735.91 cm³

5. Question

The surface area of a sphere is (576π) cm². Find its volume.

Answer

Given,

Surface area = 576n $4\pi r^2 = 576\pi$ $r^2 = \frac{576\pi}{4\pi} = 144$ r = 12cmVolume $= \frac{4}{3}\pi r^3$ $= \frac{4}{3}\pi \times 12 \times 12 \times 12$

 $= 2304 \text{cm}^3$

6. Question

The outer diameter of a spherical shell is 12 cm and its inner diameter is 8 cm. Find the volume of metal contained in the shell. Also, find its outer surface area.

12.0

Answer

Given,

Outer Diameter of spherical shell = 12cm

Radius of the outer sphere $r_1 = 6$ cm

Inner diameter of spherical shell = 8cm

Radius of the inner sphere $r_2 = 4cm$

Volume of metal = outer volume – inner volume

$$= \frac{4}{3}\pi r_1^3 - \frac{4}{3}\pi r_2^3$$

= $\frac{4}{3}\pi [r_1^3 - r_2^3]$
= $\frac{4}{3} \times \frac{22}{7} \times [6^2 - 4^3]$
= $\frac{4}{3} \times \frac{22}{7} [216 - 64]$
= $\frac{4}{3} \times \frac{22}{7} \times 152$

 $= 636.95 \text{cm}^3$

Surface area of outer surface = $4\pi r^2$

$$= 4 \times \frac{22}{7} \times 6 \times 6$$

 $= 452.571 \text{cm}^2$

7. Question

How many lead shots, each 3 mm in diameter, can be made from a cuboid with dimensions $(12 \text{ cm} \times 11 \text{ cm} \times 9 \text{ cm})?$

Answer

Given,

Dimensions of cuboid I = 12cm

b = 11cm

h = 9cm

Diameter of sphere (d) = 3mm

$$r = \frac{3}{2}mm = 1.5mm$$

r = 0.15 cm

When we melt any object, and convert it into another then the volume of both the object will be same.

So,

Volume of cuboid = $n \times volume$ of sphere

n = no. of sphere

 $I \times b \times h = n \times \frac{4}{3} \pi r^3$

 $12 \times 11 \times 9 = n \times \frac{4}{3} \times \frac{22}{7} \times 0.15 \times 0.15 \times 0.15$

 $\frac{12 \times 11 \times 9 \times 3 \times 7 \times 100 \times 100 \times 100}{4 \times 22 \times 0.15 \times 0.15 \times 0.15}$ $3 \times 7 \times 20 \times 20 \times 20$ n =

n = 84000

8. Question

How many lead balls, each of radius 1 cm, can be made from a sphere of radius 8 cm?

2

Answer

Given,

Radius of big sphere (R) = 8cm

Radius of small sphere (r) = 1cm

Volume of big sphere = $2 \times$ volume of small sphere

n = no. of sphere

 $\frac{4}{3}\pi R^3 = n \times \frac{4}{3}\pi r^3$

$$\frac{4}{3}\pi(8)^3 = n \times \frac{4}{3}\pi(1)^3$$

512 = n

n = 512 ball

9. Question

A solid sphere of radius 3 cm is melted and then cast into smaller spherical balls, each of diameter 0.6 cm. Find the number of small balls thus obtained.

Answer

Given,

Radius of big ball = 3cm

Diameter of small ball = 0.16cm

$$r = \frac{0.16}{2} = 0.3cm$$

Volume of big ball = $n \times$ volume of small ball

$$\frac{4}{3}\pi(3)^3 = n \times \frac{4}{3}\pi(0.3)^3$$

$$n = \frac{(3)^3}{(0.3)^3} = \frac{3 \times 3 \times 3}{0.3 \times 0.3 \times 0.3} = \frac{3 \times 3 \times 3}{3 \times 3 \times 3} \times 1000$$

n = 1000

10. Question

A metallic sphere of radius 10.5 cm is melted and then recast into smaller cones, each of radius 3.5 cm and height 3 cm. How many cones are obtained?

2.05

Answer

Given,

Sphere radius = 10.5cm

Cone radius = 3.5cm

h = 3cm

When any object is melt and recast into another so the volume of both the object will be same

Volume of sphere = $n \times volume$ of cone

$$\frac{4}{3} \times \pi r^{3} = n \times \frac{1}{3} \pi r^{3} h$$

$$\frac{4}{3} \pi \times 10.5 \times 10.5 \times 10.5 = n \times \frac{1}{3} \times \pi \times 3.5 \times 3.5 \times 3$$

$$n = \frac{4\pi \times 10.5 \times 10.5 \times 10.5 \times 3}{3\pi \times 3.5 \times 3.5 \times 3}$$
11. Question

How many spheres 12 cm in diameter can be made from a metallic cylinder of diameter 8 cm and height 90 cm?

Answer

Given,

Diameter of cylinder = 8cm

Radius = 4cm

Height = 90cm

Diameter of sphere = 12cm

Radius = 6cm

When we convert any object into another shape the volume will remain same.

Volume of cylinder = $n \times volume$ of sphere

$$\pi r^2 h = n \times \frac{4}{3}\pi r^3$$

$$\pi \times 4 \times 4 \times 90 = n \times \frac{4}{2}\pi(6)^3$$

 $n = \frac{\pi \times 4 \times 4 \times 90 \times 3}{4\pi \times (6)^3}$

$$n = \frac{4 \times 90 \times 3}{6 \times 6 \times 6} = \frac{90}{18}$$

12. Question

The diameter of a sphere is 6 cm. It is melted and drawn into a wire of diameter 2 mm. Find the length of the wire.

2.0

Answer

Given,

Diameter sphere = 6cm

r = 3cm

radius of wire = $\frac{2}{2} = 1mm$

r = 0.1cm

let us consider length of wire = h cm

When we convert any object into another shape the volume will remain same.

Volume of sphere = volume of cylinder

 $\frac{4}{3}\pi r^{3} = \pi r^{2}h$ $\frac{4}{3}\pi (3)^{3} = \pi (1)^{2}h$ $h = \frac{4\pi \times 3 \times 3 \times 3}{3 \times 0.1 \times 0.1 \times \pi} = \frac{4 \times 3 \times 3}{.001}$ $h = 36 \times 100 = 3600$ h = 36m

13. Question

The diameter of a copper sphere is 18 cm. It is melted and drawn into a long wire of uniform cross section. If the length of the wire is 108 m, find its diameter.

Answer

Given, Radius of sphere = 9cm Let us consider diameter at cylinder = d cm Radius = r cm Height = 108 m = 10800 cm When we convert any object into another shape the volume will remain same. Volume of sphere = volume of cylinder $\frac{4}{3}\pi r^3 = \pi r^2 h$ $\frac{4}{3}\pi (9)^3 = \pi r^2 \times 10800$ $r^2 = \frac{4 \times 9 \times 9 \times 9}{3 \times 10800}$ $r^2 = \frac{4}{3} \times \frac{729}{10800}$ $r^2 = 0.09$ r = 0.03 cm

Diameter = $2 \times 0.03 = 0.06$ cm

14. Question

A sphere of diameter 15.6 cm is melted and cast into a right circular cone of height 31.2 cm. Find the diameter of the base of the cone.

Answer

Given,

When we convert any object into another shape the volume will remain same.

Radius of sphere = $\frac{15.6}{2} = 7.8cm$ Radius of cone = r cm Volume of sphere = volume of cone $\frac{4}{3}\pi r^3 = \frac{1}{3}\pi r^2 h$ $\frac{4}{3}\pi (7.8)^3 = \frac{1}{3}\pi r^2 \times 31.2$ $r^2 = \frac{4\pi \times 3 \times 7.8 \times 7.8 \times 7.8}{3\pi \times 31.2} = \frac{4 \times 474.552}{31.2}$ $r^2 = \frac{1898.208}{31.2}$ $r^2 = 60.84$ r = 7.8cm

 $d = 2 \times r = 2 \times 7.8 = 15.6 \text{ cm}$

15. Question

A spherical cannonball 28 cm in diameter is melted and cast into a right circular cone mould, whose base is 35 cm in diameter. Find the height of the cone.

Answer

Given,

Radius of sphere $(r_3) = 14$ cm

Diameter of cone = 35cm

$$r_{c} = \frac{35}{2}$$

When we convert any object into another shape the volume will remain same.

Volume of sphere = volume of cone

$$\begin{aligned} &\frac{4}{3}\pi r_3^3 = \frac{1}{3}\pi r_c^2 h \\ &4r_3^3 = r_c^2 \\ &4 \times (14)^3 = \left(\frac{35}{2}\right)^2 \times h \\ &h = \frac{4 \times 14 \times 14 \times 14}{\left(\frac{35}{2}\right)^2} \\ &h = \frac{4 \times 14 \times 14 \times 14 \times 2 \times 2}{35 \times 35} = 35.84cm \end{aligned}$$

16. Question

A spherical ball of radius 3 cm is melted and recast into three spherical balls. The radii of two of these balls are 1.5 cm and 2 cm. Find the radius of the third ball.

2.01

Answer

Given,

Radius of big ball (R) = 3cm

Radius of smaller ball $(r_1) = 1.5$ cm

Radius of second smaller ball $(r_2) = 2 \text{ cm}$

Let r_3 be the radius of 3^{rd} smaller ball

 $V = v_1 + v_2 + v_3$

 $\frac{4}{3}\pi(R)^3 = \frac{4}{3}\pi r_1^3 + \frac{4}{3}\pi r_2^3 + \frac{4}{3}\pi r_3^3$ $(R)^3 = r_1^3 + r_2^3 + r_3^3$ $(3)^3 = (1.5)^3 + (2)^3 + (r_3)^3$ $27 = 2.817 + 8 + (r_3)^3$

$$(r_3)^3 = 27 - (2.817 + 8) = 16.875$$

 $r_3 = 2.5 \text{ cm}$

17. Question

The radii of two spheres are in the ratio 1:2. Find the ratio of their surface areas.

Answer

Given,

Ratio of radii of spheres = R_1 : R_2 = 1 : 2

Ratio of their surface areas $=\frac{A_1}{A_2} = \frac{4\pi R_1^2}{4\pi R_2^2} = \frac{R_1^2}{R_2^2} = \left(\frac{1}{2}\right)^2 = \frac{1}{4}.$

18. Question

The surface areas of two spheres are in the ratio 1:4. Find the ratio of their volumes.

Answer

Given,

Ratio of Surface area of two spheres = A_1 : $A_2 = 1 : 4$

Let radius of these sphere are resp. = R_1 and R_2

$$=\frac{A_1}{A_2}=\frac{1}{4}$$

$$= \frac{4\pi R_1^2}{4\pi R_2^2} = \frac{1}{4}$$
$$= \frac{R_1^2}{R_2^2} = \frac{1}{4}$$
$$= \frac{R_1}{R_2} = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

Ratio of their volumes $=\frac{\frac{4}{3}\pi R_1^3}{\frac{4}{3}\pi R_2^3} = \frac{R_1^3}{R_2^3} = \left(\frac{1}{2}\right)^3 = \frac{1}{8}.$

19. Question

A cylindrical tub of radius 12 cm contains water to a depth of 20 cm. A spherical iron ball is dropped into the tub and thus the level of water is raised by 6.75 cm. What is the radius of the ball?

Answer

Given, Radius of cylinder = 12 cm Height = 20 cm Before drop a ball volume of water = $v_1 = \pi r^2 h = \pi r^2 \times 20 \text{ cm}^3$ After droping rise in water level = 6.75 cm New height = 20 + 6.75 = 26.75 cm New volume = $\pi r^2 \times 26.75 \text{ cm}^3$ Volume of spherical ball = $\pi r^2 (26.75 - 20)$ = $\pi r^2 \times 6.75 = \frac{22}{7} \times 12 \times 12 \times 6.75 = 3054.85 \text{ cm}^3$ = $\frac{4}{3} \pi R^3 = 3054.85$ = $R^3 = \frac{3054.85 \times 3 \times 7}{4 \times 22} = 729$ = $R = \sqrt[3]{729} = 9 \text{ cm}$

20. Question

A cylindrical bucket with base radius 15 cm is filled with water up to a height of 20 cm. A heavy iron spherical ball of radius 9 cm is dropped into the bucket to submerge completely in the water. Find the increase in the level of water.

Answer

Given,

Radius of spherical ball = 9 cm

Volume of spherical ball = $\frac{4}{3}\pi r^3 = \frac{4}{3}\pi (9)^3 cm^3$

Radius of cylinder = 15 cm

Let the increase in level = h cm

$$= \frac{4}{3} \pi \times 729 = \pi \times 15 \times 15 \times h$$
$$= h = \frac{4}{3} \times \frac{729}{225} = 4.326 \, cm$$

21. Question

A hemisphere of lead of radius 9 cm is cast into a right circular cone of height 72 cm. Find the radius of the base of the cone.

Answer

Given, Radius of hemisphere = (R) = 9 cm Height of cone = 72 cm Let radius of cone = r cm We know that, Volume of hemisphere = volume of cone $= \frac{2}{3} \pi R^3 = \frac{1}{3} \pi r^2 h$ $= \frac{2}{3} \times 9^3 = r^2 \times 72$ $= r^2 = \frac{2 \times 729}{3 \times 72} = \frac{81}{4}$ $= r = \sqrt{\frac{81}{4}} = \frac{9}{2} = 4.5 cm$

Radius of base of cone = 4.5 cm.

22. Question

A hemispherical bowl of internal radius 9 cm contains a liquid. This liquid is to be filled into cylindrical shaped small bottles of diameter 3 cm and height 4 cm. How many bottles are required to empty the bowl?

Answer

Given,

Radius of hemisphere (R) = 9 cm

Radius of cylinder (r) = $\frac{3}{2} = 1.5 \ cm$

Height of cylinder = 4 cm

Volume of hemisphere = $n \times volume$ of cylinder

$$= \frac{2}{3} n R^{3} = n \times n r^{2} h$$
$$= \frac{2}{3} \times 9^{3} = n \times 1.5^{2} \times 4$$
$$= n = \frac{2 \times 9 \times 9 \times 9}{3 \times 1.5 \times 1.5 \times 4} = 54.$$

23. Question

A hollow spherical shell is made of a metal of density 4.5 g per cm³. If its internal and external radii are 8 cm and 9 cm respectively, find the weight of the shell.

Answer

Given,

Internal radius of sphere $(r_i) = 8 \text{ cm}$

External radius of sphere $(r_e) = 9 \text{ cm}$

Volume of shell = (external volume - internal volume)

$$=\frac{4}{3}\pi r_e^3 - \frac{4}{3}\pi r_i^3 = \frac{4}{3}\pi (9^3 - 8^3) = \frac{4}{3} \times \frac{22}{7} \times 217 = 909.33 \text{ cm}^3$$

Weight of sphere = $909.33 \times 4.5 = 4092$ gm = 4.092 kg

24. Question

A hemispherical bowl is made of steel 0.5 cm thick. The inside radius of the bowl is 4 cm. Find the volume of steel used in making the bowl.

Answer

Given,

In-radius of bowl $(r_i) = 4 \text{ cm}$

Thickness of steel = 0.5 cm

External radius of bowl $(r_e) = 4 + 0.5 = 4.5$ cm

Volume of metal = $\frac{2}{3}\pi r_e^3 - \frac{2}{3}\pi r_i^3$

$$= \frac{2}{3}\pi (r_e^3 - r_i^3) = \frac{2}{3}\pi (4.5^3 - 4^3) = \frac{2}{3} \times \frac{22}{7} \times (91.25 - 64)$$
$$= \frac{2}{3} \times \frac{22}{7} \times 27.125 = 56.83 \text{ cm}^3$$

CCE Questions

1. Question

The length, breadth and height of a cuboid are 15 cm, 12 cm, and 4.5 cm respectively. Its volume is

A. 243 cm³

B. 405 cm³

C. 810 cm³

D. 603 cm³

Answer

Given: Length = 15 cm

Breadth = 12 cm

Height = 4.5 cm

Volume of a cuboid = Length × Breadth × Height

Volume = 15 cm \times 12 cm \times 4.5 cm = 810 cm³

2. Question

A cuboid is 12 cm long, 9 cm broad and 8 cm high. Its total surface area is

odini

A. 864 cm²

B. 552 cm²

C. 432 cm²

D. 276 cm²

Answer

Given: Length = 12 cm

Breadth = 9 cm

Height = 8 cm

```
Total surface area of a cuboid = 2[(Length ×Breadth) + (Breadth ×Height) + (Height ×Length)]
```

Total surface area = $2[(12 \times 9) + (9 \times 8) + (8 \times 12)]$ cm² = 2(108 + 72 + 96) cm²

 $= 2(276) \text{ cm}^2 = 552 \text{ cm}^2$

3. Question

The length, breadth and height of a cuboid are 15 m, 6 m and 5 dm respectively. The lateral surface area of the cuboid is

A. 45 m²

B. 21 m²

C. 201 m²

D. 90 m²

Answer

Given: Length = 15 m

Breadth = 6 m

Height = 5 m

Lateral surface area of a cuboid = $2(\text{Length +Breadth}) \times \text{Height}$

1 m = 10 dm

⇒ 5dm =0.5m

Lateral surface area = $2(15+6) \times 0.5 \text{ m}^2 = 1 \times 21 \text{ m}^2$

 $= 21 \text{ m}^2$

4. Question

A beam 9 m long, 40 cm wide and 20 cm high is made up of iron which weighs 50 kg per cubic metre. The weight of the beam is

311

- A. 27 kg
- B. 48 kg
- C. 36 kg
- D. 56 kg

Answer

Given: Length = 9 cm

Breadth = 40 cm

Height = 20 cm

Volume of a cuboid = Length \times Breadth \times Height

1 m =100 cm

 \Rightarrow 40 cm= 0.4 m and 20 cm =0.2 m

Volume = 9 m × 0.4m × 0.2m = 0.72 m³

Given that 1 cm³ weighs 50 kg

 \Rightarrow 0.72 m³ weighs 50 \times 0.72 kg = 36 kg

5. Question

The length of the longest rod that can be placed in a room of dimensions ($10m \times 10m \times 5m$) is

A. 15 m

B. 16 m

C. 10√5 m

D. 12 m

Answer

Longest rod = diagonal of the cuboid = $\sqrt{(l^2 + b^2 + h^2)}$

Length of longest rod = $\sqrt{(10^2 + 10^2 + 5^2)} = \sqrt{(100 + 100 + 25)}$

 $=\sqrt{225} = 15m$

6. Question

What is the maximum length of a pencil that can be placed in a rectangular box of dimensions (8cm × 6cm × 5cm)?(Given $\sqrt{5} = 2.24$)

12.

- A. 8 cm
- B. 9.5 cm
- C. 19 cm
- D. 11.2 cm

Answer

Maximum length of a pencil = diagonal of the cuboid

Now, the diagonal of cuboid is = $\sqrt{l^2 + b^2 + h^2}$

Thus,

Length of longest rod

 $=\sqrt{(8^2+6^2+5^2)}$

$$=\sqrt{(64+36+25)}$$

=
$$\sqrt{125}$$

= 5√5 cm

= 5(2.24) cm

= 11.2 cm

7. Question

The number of planks of dimensions ($4m \times 5m \times 2m$) that can be stored in a pit which is 40, long 12 m wide and 16 m deep, is

A. 190

B. 192

C. 184

D. 180

Answer

Volume of a cuboid = Length \times Breadth \times Height

Volume of pit = 40 m × 12 m × 16 m = 7680 m³

Volume of plank = 4 m \times 5 m \times 2 m = 40 m³

No. of planks = $\frac{\text{Volume of Pit}}{\text{volume of Plank}} = \frac{7680}{40}$

= 192

8. Question

How many planks of dimensions $(5m \times 25cm \times 10cm)$ can be stored in a pit which is 20 m long, 6 m wide and 50 cm deep?

- A. 480
- B. 450
- C. 320
- D. 360

Answer

Volume of a cuboid = Length × Breadth × Height

1 m =100 cm

Volume of pit = 20 m × 6 m × 0.5 m = 60 m³

Volume of plank = $5 \text{ m} \times 0.25 \text{ m} \times 0.1 \text{ m} = 0.125 \text{ m}^3$

No. of planks = $\frac{\text{Volume of Pit}}{\text{volume of Plank}} = \frac{60}{0.125}$

= 480

9. Question

How many bricks will be required to construct a wall 8 m long, 6 m high and 22.5 cm thick if each brick measures (25cm \times 11.25 cm \times 6cm)?

A. 4800

B. 5600

C. 6400

D. 5200

Answer

Volume of a cuboid = Length \times Breadth \times Height

1 m =100 cm

Volume of wall = $8 \text{ m} \times 6 \text{ m} \times 0.225 \text{ m} = 10.8 \text{ m}^3$

Volume of a brick = $0.25 \text{ m} \times 0.1125 \text{ m} \times 0.06 \text{ m} = 0.0016875 \text{ m}^3$

No. of bricks = $\frac{\text{Volume of wall}}{\text{volume of brick}}$ $=\frac{10.8}{0.0016875}$

= 6400

10. Question

How many persons can be accommodated in a dining hall of dimensions $(20m \times 15m \times 4.5m)$, assuming that each person requires 5m³ of air?

- A. 250
- B. 270
- C. 320
- D. 300

Answer

Volume of a cuboid = Length \times Breadth \times Height

```
Volume of hall = 20 m × 15 m × 4.5 m = 1350 m<sup>3</sup>
```

Volume of air required by 1 person = 5 m^3

Volume of hall No. of persons = $\frac{Volume of han}{Volume of air required by 1 person} = \frac{1}{V}$

=270

11. Question

A river 1.5 m deep and 30 m wide is flowing at the rate of 3 km per hour. The volume of water that runs into the sea minute is

- A. 2000 m³
- B. 2250 m³
- C. 2500 m³
- D. 2750 m³

Answer

Volume of a cuboid = Length \times Breadth \times Height

Length of the river = Speed of river = 3km (in an hr)

1km =1000 m and 1 hour =60 min

Speed in m per minute = $3 \times \frac{1000}{60} = 50 \text{m per min}$

Volume of water that runs in a minute = $1.5 \text{ m} \times 30 \text{ m} \times 50 \text{ m} = 2250 \text{ m}^3$

12. Question

The lateral surface area of a cube is 256m². The volume of the cube is

- A. 64 m³
- B. 216 m³
- C. 256 m³
- D. 512 m³

Answer

Lateral surface area of a cube = $4(side)^2$

Given Lateral surface area = 256 m^2

 \Rightarrow 4(side)² = 256m²

$$\Rightarrow$$
 (side)² = $\frac{256}{m}$ m²

- \Rightarrow (side) = $\sqrt{64m}$ = 8m
- Volume of a cube = $(side)^3$

 \Rightarrow Volume = (8)³ m³ = 512 m³

13. Question

The total surface area of a cube is 96 cm^2 . The volume of the cube is

A. 8 cm³

B. 27 cm³

C. 64 cm³

D. 512 cm³

Answer

Total surface area of a cube = $6(side)^2$ Given Total surface area = 96 cm^2 $\Rightarrow 6(side)^2 = 96m^2$ $\Rightarrow (side)^2 = \frac{96}{6} \text{cm}^2$ $\Rightarrow (side) = \sqrt{16} \text{cm} = 4 \text{cm}$ Volume of a cube = $(side)^3$ $\Rightarrow \text{Volume} = (4)^3 \text{ cm}^3 = 64 \text{ cm}^3$

14. Question

The volume of a cube is 512 cm^3 . Its total surface area is

- A. 256 cm²
- B. 384 cm²
- C. 512 cm²
- D. 64 cm²

Answer

Volume of a cube = $(side)^3$

Given volume = 512 cm^3

- \Rightarrow (side)³ = 512 cm³
- \Rightarrow side = $\sqrt[3]{512}$ = 8 cm

Total surface area of a cube = $6(side)^2$

 \Rightarrow Total surface area = 6(8)² cm² = 384 cm²

15. Question

The length of the longest rod that can fit in a cubical vessel of side 10 cm, is

A. 10 cm

B. 20 cm

C. 10√2 cm

D. 10√3 cm

Answer

Length of the longest rod = diagonal of the cube = side $\sqrt{3}$

Length of longest rod =10 $\sqrt{3}$ cm

16. Question

If the length of diagonal of a cube is $8\sqrt{3}$ cm, then its surface area is

- A. 192 cm²
- B. 384 cm²
- C. 512 cm²
- D. 768 cm²

Answer

Diagonal of the cube = side $\sqrt{3}$

Given diagonal =8 $\sqrt{3}$ cm = side $\sqrt{3}$

 \Rightarrow side = 8 cm

Total surface area of a cube = $6(side)^2$

 \Rightarrow Surface area = 6(8)² = 6×64 = 384 cm²

17. Question

If each edge of a cube is increased by 50%, then the percentage increase in its surface area is

A. 50%

- B. 75%
- C. 100%
- D. 125%

Answer

Let original side be x, on increasing it by 50% i.e. $\frac{50}{100} = \frac{1}{2}$

New side will be $x + \frac{1}{2}x = \frac{3}{2}x$

Total surface area of a cube = $6(side)^2$

Original surface area = $6 (x)^2$

New surface area = $6(\frac{3}{2}x)^2 = 6 \times \frac{9}{4}x^2 = \frac{27}{2}x^2$

Change in surface area = $\frac{27}{2}x^2 - 6(x)^2$

Taking LCM of 2 and 1 = 2

$$\Rightarrow \frac{27x^2 - 12x^2}{2} = \frac{15}{2}x^2$$

The percentage increase in its surface area is $\frac{\frac{15}{2}x^2}{6x^2} \times 100\% = 125\%$

18. Question

Three cubes of metal with edges 3 cm, 4 cm and 5 cm respectively are melted to form a single cube. The lateral surface area of the new cube formed is

- A. 72 cm²
- B. 144 cm²
- C. 128 cm²
- D. 256 cm²

Answer

Here, the volume of three cubes = volume of the new cube

Volume of a cube = $(side)^3$

Volume of three cubes = $(3)^3 + (4)^3 + (5)^3 = (27 + 64 + 125) \text{ cm}^3 = 216 \text{ cm}^3$

- \Rightarrow Volume of new cube = 216 cm³ = (side)³
- \Rightarrow (side)³ = (6 cm)³
- \Rightarrow side = 6cm

Lateral surface area =
$$4(side)^2 = 4(6)^2 = 144$$
cm²

19. Question

In a shower, 5 cm of rain falls. What is the volume of water that falls on 2 hectares of ground?

- A. 500 m³
- B. 750 m³
- C. 800 m³
- D. 1000 m³

Answer

- $1 \text{ hectare} = 10000 \text{ m}^2$
- 2 hectares = 20000 m^2

 $1 \text{ cm} = 0.01 \text{ m} \Rightarrow 5 \text{ cm} = 0.05 \text{ m}$

Volume of water that falls on 2 hectares of ground = $20000 \times 0.05 \text{ m}^3 = 1000 \text{ m}^3$

20. Question

Two cubes have their volumes in the ratio 1 : 27. The ratio of their surface areas is

A.1:3

B.1:8

C.1:9

D. 1 : 18

Answer

Volume of a cube = $(side)^3$

Let the sides be x and y

Ratio of volumes $=\frac{x^3}{y^3}=\frac{1}{27}$

$$\Rightarrow \frac{x}{y} = \frac{1}{3}$$

Surface area of a cube = $6(side)^2$

Ratio of surface areas $=\frac{x^2}{y^2}=\frac{1}{3^2}=\frac{1}{9}=1:9$

21. Question

If each side of a cube is doubled, then its volume

A. is doubled

B. becomes 4 times

C. becomes 6 times

D. becomes 8 times

Answer

Let original side be x, New side will be 2x

Volume of a cube = $(side)^3$

Original volume = $(x)^3$

New volume = $(2x)^3 = 8x^3$

So, the volume is 8 times of the original volume

22. Question

The diameter of the base of a cylinder is 6 cm and its height is 14 cm. The volume of the cylinder is

A. 198 cm³

B. 396 cm³

C. 495 cm³

D. 297 cm³

Answer

Volume of a cylinder = $\pi r^2 h$

Diameter = $6 \text{cm} \Rightarrow \text{radius} = 3 \text{cm}$

 \Rightarrow Volume = $\frac{22}{7} \times 3^2 \times 14$

 $= 22 \times 9 \times 2 = 396 \text{cm}^3$

23. Question

If the diameter of a cylinder is 28 cm and its height is 20 cm, then its curved surface area is

- A. 880 cm²
- B. 1760 cm²
- C. 3520 cm²
- D. 2640 cm²

Answer

Curved surface area of a cylinder = $2\pi rh$

Diameter = 28 cm \Rightarrow radius = 14 cm

⇒ Curved surface area = $2 \times \frac{22}{7} \times 14 \times 20$

 $= 44 \times 40 = 1760 \text{ cm}^2$

24. Question

If the curved surface area of a cylinder is 1760 cm² and its base radius is 14 cm, then its height is

A. 10 cm

B. 15 cm

C. 20 cm

D. 40 cm

Answer

Curved surface area of a cylinder = $2\pi rh$

 \Rightarrow Curved surface area = 2 $\times \frac{22}{7} \times 14 \times h = 1760 \text{ cm}^2$ \Rightarrow h = $\frac{1760}{44 \times 2}$ = 20 cm

25. Question

The height of a cylinder is 14 cm and its curved surface area is 264 cm². The volume of the cylinder is

- A. 308 cm³
- B. 396 cm³
- C. 1232 cm³
- D. 1848 cm³

Answer

Curved surface area of a cylinder = $2\pi rh$

 \Rightarrow Curved surface area = 1760 cm²

$$\Rightarrow 2 \times \frac{22}{7} \times r \times 14 = 1760 \text{ cm}^2$$

$$\Rightarrow r = \frac{1760}{44 \times 2} = 20 \text{ cm}$$

Volume of a cylinder = $\pi r^2 h$

Volume = $\frac{22}{7} \times 20^2 \times 14$

 $= 17,600 \text{ cm}^3$

26. Question

The curved surface area of a cylindrical pillar is 264 m² and its volume is 924 m³. The height of the pillar is

- A. 4 m
- B. 5 m
- C. 6 m
- D. 7 m

Answer

Curved surface area of a cylinder = $2\pi rh$

 \Rightarrow Curved surface area = 2 $\times \frac{22}{7} \times r \times h = 264 \text{ m}^2$

$$\Rightarrow r = \frac{264 \times 7}{44 \times h} = \frac{42}{h}$$

Volume of a cylinder = $\pi r^2 h$

Volume =
$$\frac{22}{7} \times \left(\frac{42}{h}\right)^2 \times h = 924 \text{m}^3$$

 $\Rightarrow h = \frac{22 \times 42 \times 6}{924}$
 $\Rightarrow h = \frac{42 \times 6}{42} = 6 \text{ m}$

27. Question

The radii of two cylinders are in the ratio 2 :3 and their heights are in the ratio 5 :3. The ratio of their curved surface area is

A. 2 : 5

B.8:7

C. 10:9

D. 16 : 9

Answer

Let the radii be 2x and 3x respectively and heights be 5y and 3y respectively.

Curved surface area of a cylinder = $2\pi rh$

 \Rightarrow Ratio of their Curved surface area = $\frac{2\pi rh}{2\pi RH} = \frac{2x \times 5y}{3x \times 3y} = \frac{10}{9}$

28. Question

The radii of two cylinders are in the ratio 2 : 3 and their heights are in the ratio 5:3. The ratio of their volumes is

A. 27:20

B. 20 : 27

C. 4:9

D.9:4

Answer

Let the radii be 2x and 3x respectively and heights be 5y and 3y respectively.

Volume of a cylinder = $\pi r^2 h$

 \Rightarrow Ratio of their Volumes $=\frac{\pi r^2 h}{\pi R^2 H} = \frac{2x^2 \times 5y}{3x^2 \times 3y} = \frac{20}{27}$

29. Question

The ratio between the radius of the base and the height of a cylinder is 2 : 3. If its volume is 1617 cm³, then its total surface area is

A. 308 cm²

B. 462 cm²

C. 540 cm²

D. 770 cm²

Answer

Let the radius be 2x and height be 3x respectively.

Volume of a cylinder = $\pi r^2 h$

$$\Rightarrow \text{Volume} = \frac{22}{7} \times (2x)^2 \times 3x = 1617$$

$$\Rightarrow \frac{22}{7} \times x^3 \times 12 = 1617$$

$$\Rightarrow x^{3} = \frac{1617 \times 7}{22 \times 12} = \frac{343}{8}$$

$$\Rightarrow x = \frac{7}{2} = 3.5$$

So, radius = $2 \times 3.5 = 7$ cm and height = $3 \times 3.5 = 10.5$ cm

Total surface area of a cylinder = $2\pi r(r + h)$

⇒ T.S.A. =
$$2 \times \frac{22}{7} \times 7(7 + 10.5) = 44 \times 17.5 = 770 \text{ cm}^2$$

30. Question

Two circular cylinders of equal volume have their heights in the ratio 1 : 2. The ratio of their radii is

- A. 1:√2 B. $\sqrt{2}$: 1
- C. 1:2
- D.1:4

Answer

Let the heights be h = x and H=2x respectively of the two cylinders.

Volume of a cylinder = $\pi r^2 h$

Given that $\pi r^2 h = \pi R^2 H$

$$\Rightarrow \frac{r^2}{R^2} = \frac{2x}{x}$$
$$\Rightarrow r: R = \sqrt{2}: 1$$

31. Question

The ratio between the curved surface area and the total surface area of a right circular cylinder is 1 : 2. If the total surface area is 616 cm^2 , then the volume of the cylinder is

2.0

- A. 1078 cm³
- B. 1232 cm³
- C. 1848 cm³
- D. 924 cm³

Answer

Total surface area of a cylinder = $2\pi r(r + h)$

Curved surface area of a cylinder = $2\pi rh$

$$\Rightarrow \frac{2\pi rh}{2\pi r(r+h)} = \frac{1}{2}$$

 \Rightarrow 2h=r + h \Rightarrow h = r

Given that total surface area = 616 cm

$$\Rightarrow 2 \times \frac{22}{7} \times 2r^2 = 616$$

 \Rightarrow r² = 7 × 7

So, r = h = 7 cm

Volume of a cylinder = $\pi r^2 h$

$$\Rightarrow \frac{22}{7} \times 49 \times 7 = 1078 \text{ cm}^3$$

32. Question

In a cylinder, if the radius is halved and the height is doubled, then the volume will be

A. the same

B. doubled

C. halved

D. four times

Answer

Let the radius be r and height be h

Volume of a cylinder = $\pi r^2 h$

When radius = $\frac{1}{2}$ r and height = 2h

Volume = $\pi \left(\frac{r}{2}\right)^2 \times 2h = \pi \frac{r^2}{2}h$

The volume will be halved.

33. Question

The number of coins 1.5 cm in diameter and 0.2 cm thick to be melted to form a right circular cylinder of height 10 cm and diameter 4.5 cm is

A. 540

- B. 450
- C. 380
- D. 472

Answer

Volume of a cylinder = $\pi r^2 h$

Volume of the coin =
$$\pi (\frac{1.5}{2})^2 \times 0.2$$

Volume of the cylinder = π $^{2} \times 10^{2}$

Number of coins = $\frac{\text{Volume of the cylinder}}{\text{Volume of the coin}}$

$$= \frac{\pi \left(\frac{4.5}{2}\right)^2 \times 10}{\pi \left(\frac{1.5}{2}\right)^2 \times 0.2}$$

 $= 9 \times 50 = 450$

34. Question

The radius of a wire is decreased to one-third. If volume remains the same, the length will become

A. 2 times

B. 3 times

C. 6 times

D. 9 times

Answer

Let radius and length of a wire be r and h respectively

Volume of a wire = $\pi r^2 h$

If radius = $\frac{r}{3}$ and new length = H

Volume of the wire = $\pi (\frac{r}{2})^2 \times H = \pi r^2 h$

 \Rightarrow H = 9h i.e. 9 times

35. Question

The diameter of a roller, 1 m long, is 84 cm. If it takes 500 complete revolutions to level a playground, the area of the playground is

ka.

A. 1440 m²

B. 1320 m²

- C. 1260 m²
- D. 1550 m²

Answer

Curved surface area of a cylinder = $2\pi rh$

1m= 100cm, radius = 42 cm = 0.42m

```
Curved surface area = 2 \times \frac{22}{7} \times 0.42 \times 1 = 2.64 \text{ m}^2
```

Area of the playground = $500 \times 2.64 \text{ m}^2 = 1320 \text{ m}^2$

36. Question

2.2 dm³ of lead is to be drawn into a cylindrical wire 0.50 cm in diameter. The length of the wire is

A. 110 m

- B. 112 m
- C. 98 m
- D. 12 m

Answer

Given volume of the cylindrical wire is 2.2dm³

Volume of a wire = $\pi r^2 h$

 $1 \text{ dm} = 10 \text{ cm} \Rightarrow 0.50 \text{ cm} = 0.05 \text{ dm}$

Volume of the wire = $\pi (0.25)^2 \times \text{length of the wire} = 2.2$

$$\Rightarrow h = \frac{2.2 \times 7}{22 \times 0.0625} = 11.2 \text{ dm}$$

1 m= 10 dm

⇒ 11.2 dm = 112 m

37. Question

The lateral surface area of a cylinder is

A. $\pi r^2 h$

B. *πrh*

C. 2πrh

D. 2πr²

Answer

The curved surface area of a cylinder is only the lateral surface area

And, we know that the curved surface area = $2\pi rh$

38. Question

The height of a cone is 24 cm and the diameter of its base is 14 cm. The curved surface area of the cone is

A. 528 cm²

B. 550 cm²

C. 616 cm²

D. 704 cm²

Answer

Curved surface area of a cone = πrl

where $l = \sqrt{h^2 + r^2}$

Here, r=7cm and h=24cm

$$l = \sqrt{24^2 + 7^2}$$

$$=\sqrt{625}$$

= 25cm

$$\Rightarrow \frac{22}{7} \times 7 \times 25$$

 $= 550 \text{cm}^2$

39. Question

The volume of a right circular cone of height 12 cm and base radius 6 cm, is

- A. (12π) cm³
- B. (36π) cm³
- C. (72π) cm³
- D. (144π)cm³

Answer

Volume of a cone = $\frac{1}{3}\pi r^2 h$

$$\Rightarrow \frac{1}{3}\pi 6^2 12$$

 $= \pi \times 36 \times 4$

```
= (144\pi) \text{cm}^3
```

40. Question

How much cloth 2.5 m wide will be required to make a conical tent having base radius 7 m and height 24 m?

A. 120 m

B. 180 m

C. 220 m

D. 550 m

Answer

Curved surface area of a cone = πrl

where $l = \sqrt{h^2 + r^2}$

Here, r=7m and h=24m

 $l = \sqrt{24^2 + 7^2}$

 $=\sqrt{625}$

= 25m

$$\Rightarrow \frac{22}{7} \times 7 \times 25 = 550 \text{m}^2$$

The cloth required $=\frac{550}{2.5}$

= 220 m

41. Question

The volume of a cone is 1570 cm^3 and its height is 15 cm. What is the radius of the cone? (Use $\pi = 3.14$)

- A. 10 cm
- B. 9 cm
- C. 12 cm
- D. 8.5 cm

Answer

Volume of a cone = $\frac{1}{2}\pi r^2 h$

Given volume = 1570 cm^3

$$\Rightarrow \frac{1}{3}\pi r^2 \times 15 = 3.14 \times r^2 \times 5 = 15.7r^2 \text{ cm}^3$$

 $\Rightarrow 15.7r^2 = 1570$

 \Rightarrow r² = 100 \Rightarrow r = 10cm

42. Question

m³ b+ The height of a cone is 21 cm and its slant height is 28 cm. The volume of the cone is

A. 7356 cm³

- B. 7546 cm³
- C. 7506 cm³
- D. 7564 cm³

Answer

Volume of a cone = $\frac{1}{3}\pi r^2 h$

where slant height $l = \sqrt{h^2 + r^2}$

Here, I=28 cm and h=21 cm

$$r = \sqrt{28^2 - 21^2}$$
$$= \sqrt{441}$$
$$= 21 \text{cm}$$
$$\text{Volume} = \frac{1}{3} \times \frac{22}{7} \times 21^2 \times 21$$
$$= 7546 \text{ cm}^3$$

43. Question

The volume of a right circular cone of height 24 cm is 1232 cm³. Its curved surface area is

- A. 1254 cm²
- B. 704 cm²
- C. 550 cm²

$$\Rightarrow \frac{1}{3} \times \frac{22}{7} \times r^2 \times 24 = 1232 \text{ cm}^3$$

 \Rightarrow r =7 cm

Curved surface area of a cone = πrl

$$\Rightarrow \frac{22}{7} \times 7 \times 25$$
$$= 550 \text{ cm}^2$$

44. Question

D. 462 cm² Answer Given: Volume of cone = 1232 cm^3 As we know, Volume of a cone = $\frac{1}{3}\pi r^2 h$ $\Rightarrow r^2 = 49$ slant height $l = \sqrt{h^2 + r^2}$ Here, r = 7 cm and h = 24 cm $l = \sqrt{7^2 + 24^2} = \sqrt{625} = 25 cm$ 5

If the volumes of two cones be in the ratio 1 : 4. and the radii of their bases be in the ratio 4 : 5, then the ratio of their heights is

con

A.1:5

B. 5:4

C. 25:16

D. 25:64

Answer

Volume of a cone = $\frac{1}{2}\pi r^2 h$

$$\Rightarrow \frac{\frac{1}{2}\pi r^{2}h}{\frac{1}{2}\pi R^{2}H} = \frac{1}{4} \text{ and } \frac{r^{2}}{R^{2}} = \frac{16}{25}$$
$$\Rightarrow \frac{h}{H} = \frac{1 \times 25}{4 \times 16}$$
$$\Rightarrow \frac{h}{H} = \frac{25}{64}$$

45. Question

If the height of a cone is doubled, then its volume is increased by

- A. 100%
- B. 200%
- C. 300%
- D. 400%

Answer

Volume of a cone = $\frac{1}{3}\pi r^2 h$

If height is doubled,

volume =
$$\frac{1}{3}\pi r^2 \times 2h$$

Volume = $\frac{2}{3}\pi r^2h$

Increase in volume = $\frac{\frac{2}{3}\pi r^2 h - \frac{1}{3}\pi r^2 h}{\frac{1}{3}\pi r^2 h} \times 100\%$

$$=\frac{\frac{1}{3}\pi r^{2}h}{\frac{1}{3}\pi r^{2}h}\times 100\%$$

= 100%

Thus, there will be 100% increase in the volume.

46. Question

The curved surface area of one cone is twice that of the other while the slant height of the latter is twice that of the former. The ratio of their radii is

A.2:1

B.4:1

C.8:1

D. 1 : 1

Answer

Curved surface area of a cone = πrl

Given that curved surface area of $1^{st} = 2 \times curved$ surface area of 2^{nd}

And slant height of $2^{nd} = 2 \times$ slant height of 1^{st}

 \Rightarrow L= 2I

 $\Rightarrow \frac{\pi r l}{\pi R L} = \frac{2}{1}$ $\Rightarrow \frac{r}{R} = \frac{2 \times 2l}{1 \times l}$

$$\Rightarrow$$
 r : R = 4 : 1

47. Question

The ratio of the volumes of a right circular cylinder and a right circular cone of the same base and the same height will be

12.C

A.1:3

B.3:1

C. 4 : 3

D. 3 :4

Answer

Given that heights and radii of cone and cylinder are equal

Volume of a cone = $\frac{1}{3}\pi R^2 H$

Volume of a cylinder = $\pi r^2 h$

Ratio of their volumes $=\frac{\pi r^2 h}{\frac{1}{2}\pi R^2 H}=\frac{3}{1}$

{because h=H and r=R}

Ans - 3:1

48. Question

A right circular cylinder and a right circular cone have the same radius and the same volume. The ratio of the height of the cylinder to that of the cone is

- A.3:5
- B. 2 : 5
- C. 3:1
- D.1:3

Answer

Let height of cylinder and cone be H and h respectively

Given that radii of cone and cylinder are equal

Volume of a cone = $\frac{1}{3}\pi r^2 h$

Volume of a cylinder = $\pi r^2 H$

Given $\frac{1}{3}\pi r^2 h = \pi r^2 H$

$$\Rightarrow \frac{H}{h} = \frac{1}{3}$$

Ans: 1:3

49. Question

The radii of the bases of a cylinder and a cone are in the ratio 3 : 4 and their heights are in the ratio 2 : 3. Then, their volumes are in the ratio

A.9:8

B.8:9

- C.3:4
- D.4:3

Answer

Given that radii of cone and cylinder are 4x and 3x respectively and

height of cylinder and cone are 2y and 3y respectively

Volume of a cone = $\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi \times 4x^2 \times 3y$

Volume of a cylinder = $\pi r^2 h = \pi \times 3x^2 \times 2y$



50. Question

If the height and the radius of a cone are doubled, the volume of the cone becomes

- A. 3 times
- B. 4 times
- C. 6 times
- D. 8 times

Answer

Volume of a cone = $\frac{1}{2}\pi r^2 h$

If height and radius are doubled, volume = $\frac{1}{3}\pi(2r)^2 \times 2h$

The volume of the cone becomes 8 times.

51. Question

A solid metallic cylinder of base radius 3 cm and height 5 cm is melted to make n solid cones of height 1 cm and base radius 1 mm. The volume of n is

 $\frac{8}{2}\pi r^2h$

- A. 450
- B. 1350

C. 4500

D. 13500

Answer

Volume of a cone = $\frac{1}{2}\pi r^2 h$

Volume of a cylinder = $\pi r^2 h$

Volume of solid metallic cylinder = $\pi(3)^2 \times 5 = 45\pi \text{ cm}^3$

1cm=10mm

Volume of solid coin = $\frac{1}{3} \pi (0.1)^2 \times 1 = \frac{1}{3} \times 0.01 \pi \text{ cm}^3$

No. of coins = $\frac{\text{Volume of solid metallic cylinder}}{\text{Volume of solid coin}}$ = $\frac{45\pi \times 3 \text{ cm}^3}{0.01\pi \text{ cm}^3}$

= 13500

52. Question

A conical tent is to accommodate 11 persons such that each person occupies $4m^2$ of space on the ground. They have 220 m³ of air to breathe. The height of the cone is

- A. 14 m
- B. 15 m
- C. 16 m
- D. 20 m

Answer

As each person needs 4 m ² spaces on ground, so 11 persons will need 44 m ² space on the ground. Therefore, Area of ground = 44 m $^2 \Rightarrow \pi r^2 = 44$

$$\Rightarrow \frac{22 \times r^2}{7} = 44$$

 \Rightarrow r² = 14Each person needs = $\frac{220}{11}$ = 20m³ of air Therefore volume of tent = 220 m³

Volume of a cone = $\frac{1}{3}\pi r^2 h \Rightarrow \frac{1}{3}\pi r^2 h = 220$ $\Rightarrow \frac{1}{3} \times \frac{22}{7} \times 14 \times h = 220$

⇒ h = 15cm

53. Question

The volume of a sphere of radius 2r is

A.
$$\frac{32\pi r^{3}}{3}$$

B. $\frac{16\pi r^{3}}{3}$
C. $\frac{8\pi r^{3}}{3}$

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume $=\frac{4}{3}\pi(2r)^3 = \frac{32}{3}\pi r^3$

54. Question

The volume of a sphere of radius 10.5 cm is

A. 9702 cm³

B. 4851 cm³

C. 19404 cm³

D. 14553 cm³

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume = $\frac{4}{3}\pi(10.5)^3$

$$=\frac{4}{3}\times\frac{22}{7}\times(10.5)^3$$

 $= 4851 \text{cm}^3$

55. Question

The surface area of a sphere of radius 21 cm is

A. 2772 cm²

B. 1386 cm²

- C. 4158 cm²
- D. 5544 cm²

Answer

Surface area of a sphere $= 4\pi r^2$

Surface area = $4\pi(21)^2$

 $= 4 \times \frac{22}{7} \times (21)^2$

```
= 5544 cm<sup>2</sup>
```

56. Question

The surface area of a sphere is 1386 cm². Its volume is

A. 1617 cm³

B. 3234 cm³

C. 4851 cm³

D. 9702 cm³

Answer

Surface area of a sphere $= 4\pi r^2$

Given Surface area = 1386 cm^2 $\Rightarrow 4 \times \frac{22}{7} \times r^2 = 1386$ $\Rightarrow r^2 = \frac{1386 \times 7}{88} = \frac{441}{4}$ $\Rightarrow r = \frac{21}{2}$ Volume of a sphere $=\frac{4}{3}\pi r^3$ Volume $=\frac{4}{2}\pi\left(\frac{21}{2}\right)^3$ $=\frac{4}{2}\times\frac{22}{7}\times\left(\frac{21}{2}\right)^3$ $= 4851 \text{cm}^3$

57. Question

If the surface area of a sphere is $(144\pi)m^2$, then its volume is

- A. (288π) m³
- B. (188π) m³
- C. (300π) m³

D. (316π) m³

Answer

Surface area of a sphere $= 4\pi r^2$

Given Surface area = (144π) m²,

 $\Rightarrow 4 \times \pi \times r^2 = 144\pi$

 \Rightarrow r= 6m

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume = $\frac{4}{3}\pi(6)^3 = 288\pi m^3$

58. Question

The volume of a sphere is 38808 cm³. Its surface area is

A. 5544 cm²

B. 8316 cm²

C. 4158 cm²

D. 1386 cm²

Answer

Volume of a sphere $=\frac{4}{2}\pi r^3$

Given Volume= 38808 cm3.

$$\Rightarrow \frac{4}{3}\pi r^3 = 38808$$

A. 5544 cm²
B. 8316 cm²
C. 4158 cm²
D. 1386 cm²
Answer
Volume of a sphere
$$=\frac{4}{3}\pi r^3$$

Given Volume= 38808 cm³.
 $\Rightarrow \frac{4}{3}\pi r^3 = 38808$
 $\Rightarrow r^3 = 38808 \times \frac{21}{88} = 9261$

 \Rightarrow r=21cm

Surface area of a sphere $= 4\pi r^2$

Surface area = $4 \times \frac{22}{7} (21)^2 = 5544 \text{ cm}^2$

59. Question

If the ratio of the volumes of two spheres is 1 : 8, then the ratio of their surface area is

A.1:2

B.1:4

C.1:8

D. 1 : 16
Volume of a sphere $=\frac{4}{3}\pi r^3$

Given that
$$\frac{3}{4\pi R^3}$$

$$\Rightarrow \frac{r}{R} = \frac{1}{2}$$

Surface area of a sphere $= 4\pi r^2$

$$\Rightarrow \frac{4\pi r^2}{4\pi R^2} = \frac{1}{4}$$

60. Question

A solid metal ball of radius 8 cm is melted and cast into smaller balls, each of radius 2cm. The number of such balls is

A.	8
	_

- B. 16
- C. 32
- D. 64

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume of the solid metal ball = $\frac{4}{3}\pi(8)^3$

Volume of smaller ball= $\frac{4}{3}\pi(2)^3$

No. of balls = $\frac{\text{Volume of the solid metal ball}}{\text{Volume of smaller ball}}$

$$=\frac{\frac{4}{3}\pi(8)^{3}}{\frac{4}{3}\pi(2)^{3}}$$

= 64

61. Question

A cone is 8.4 cm high and the radius of its base is 2.1 cm. It is melted and recast into a sphere. The radius of the sphere is

A. 4.2 cm

B. 2.1 cm

C. 2.4 cm

D. 1.6 cm

Answer

Volume of a cone = $\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi (2.1)^2 \times 8.4$

 $= 12.348\pi \text{ cm}^3$

On recasting a cone into sphere, the volume will remain same

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume of sphere =12.348 π cm³

$$\Rightarrow \frac{4}{3}\pi r^3 = 12.348\pi$$
$$\Rightarrow r^3 = 12.348 \times \frac{3}{4} = 9.261$$

 \Rightarrow r = 2.1cm

62. Question

A solid lead ball of radius 6 cm is melted and then drawn into a wire of diameter 0.2 cm. The length of wire is

- A. 272 m
- B. 288 m
- C. 292 m
- D. 296 m

Answer

Volume of a sphere $=\frac{4}{3}\pi r^{3} = \frac{4}{3}\pi (6)^{3} = 288\pi \text{ cm}^{3}$

On recasting a sphere into cylinder, the volume will remain same

Volume of a cylinder = $\pi r^2 h$

Radius = 0.1 cm

 $\Rightarrow \pi (0.1)^2 h = 288\pi$

$$\Rightarrow h = 288 \times \frac{1}{0.01}$$

= 28800cm

⇒ h = 288 m

63. Question

A metallic sphere of radius 10.5 cm is melted and then recast into small cones, each of radius 3.5 cm and height 3 cm. The number of such cones will be

A. 21

B. 63

C. 126

D. 130

Answer

Volume of a sphere $=\frac{4}{3}\pi r^{3} = \frac{4}{3}\pi (10.5)^{3} \text{ cm}^{3}$

Volume of a cone = $\frac{1}{3}\pi r^2 h$

$$=\frac{1}{3}\pi(3.5)^2 \times 3$$

$$= \pi (3.5)^2 \text{cm}^3$$

No. of cones $= \frac{\text{Volume of a sphere}}{\text{Volume of a cone}}$

$$=\frac{\frac{4}{3}\pi(10.5)^3}{\pi(3.5)^2}$$

= 126

64. Question

How many lead shots, each 0.3 cm in diameter, can be made from a cuboid of dimensions 9 cm \times 11 cm \times 12 cm ?

2.01

A. 7200

B. 8400

C. 72000

D. 84000

Answer

Volume of a cuboid = $1 \times b \times h = 9 \times 11 \times 12 \text{ cm}^3$

Radius of a lead shot = 0.15 cm

Volume of a lead shot
$$=\frac{4}{3}\pi r^{3} = \frac{4}{3}\pi (0.15)^{3} \text{ cm}^{3}$$

No. of lead shot $= \frac{\text{Volume of a cuboid}}{\text{Volume of a lead shot}}$

$$=\frac{9\times11\times12}{\frac{4}{3}\pi(0.15)^3}$$



= 84000

65. Question

The diameter of a sphere is 6 cm. It is melted and drawn into a wire of diameter 2 mm. The length of the wire is

coll

A. 12 mB. 18 m

C. 36 m

D. 66 m

Answer

Radius of the sphere = 3 cm

Volume of a sphere $=\frac{4}{3}\pi r^3$

$$=\frac{4}{3}\pi(3)^{3}$$

$$= 36\pi \text{ cm}^{3}$$

On recasting a sphere into cylinder wire, the volume will remain same

odini

Volume of a cylinder = $\pi r^2 h$

1cm=10mm

⇒ 2mm =0.2cm

Radius = 0.1 cm

```
\Rightarrow \pi(0.1)^2 h = 36\pi
```

 \Rightarrow h = 36 × $\frac{1}{0.01}$

 \Rightarrow h = 3600cm

 \Rightarrow h = 36 m (\because 1m =100 cm)

66. Question

A sphere of diameter 12.6 cm is melted and cast into a right circular cone of height 25.2 cm. The radius of the base of the cone is

A. 6.3 cm

B. 2.1 cm

C. 6 cm

D. 4 cm

Radius of the sphere = 6.3 cm Volume of a sphere = $\frac{4}{3}\pi r^3$ \Rightarrow Volume of a sphere = $\frac{4}{3}\pi (6.3)^3$ cm³ Volume of a cone = $\frac{1}{3}\pi r^2$ h \Rightarrow Volume of a cone = $\frac{1}{3}\pi r^2 \times 25.2$ = $8.4\pi r^2$ cm³

On recasting a sphere into a cone, volume will remain same

$$\Rightarrow 8.4\pi r^{2} = \frac{4}{3}\pi (6.3)^{3}$$
$$\Rightarrow r^{2} = \frac{4}{3}(6.3)^{3} \times \frac{1}{8.4} = 39.69$$

⇒ r = 6.3 cm

67. Question

A spherical ball of radius 3 cm is melted and recast into three spherical balls. The radii of two of these balls are 1.5 cm and 2 cm. The radius of the third ball is

con

A. 1 cm

B. 1.5 cm

C. 2.5 cm

D. 0.5 cm

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume of spherical ball $=\frac{4}{3}\pi(3)^3$ cm³

Volume of three balls $=\frac{4}{3}\pi(1.5)^3 + \frac{4}{3}\pi(2)^3 + \frac{4}{3}\pi r^3$

 $=\frac{4}{3}\pi(3.375+8+r^3)$ On recasting this sphere into three spherical balls, volume will remain same

$$\Rightarrow \frac{4}{3}\pi(3.375 + 8 + r^3) = \frac{4}{3}\pi(3)^3$$

 $\Rightarrow 11.375 + r^3 = 27$

 $\Rightarrow r^3 = 15.625$

⇒ r = 2.5 cm

68. Question

The radius of a hemispherical balloon increases from 6 cm to 12 cm as air is being pumped into it. The ratio of the surface areas of the balloons in two cases is

A.1:4

B.1:3

C. 2:3

D.1:2

Answer

Surface area of a hemisphere = $2\pi r^2$

Radii are 6cm and 12 cm respectively

Ratio of surface areas
$$=\frac{2\pi r^2}{2\pi R^2}=\frac{6^2}{12^2}=\frac{1}{4}$$

Ans 1:4

69. Question

The volumes of the two spheres are in the ratio 64 : 27 and the sum of their radii is 7 cm. The difference of their total surface areas is

C

A. 38 cm²

B. 58 cm²

C. 78 cm²

D. 88 cm²

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Given Ratio of volumes of two spheres $=\frac{64}{27}$

$$\Rightarrow \frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi R^3} = \frac{r^3}{R^3} = \frac{64}{27}$$
$$\Rightarrow \frac{r}{R} = \frac{4}{3}$$

So, r = 4x and R = 3x

Also given that the sum of radii = 7

 \Rightarrow r +R = 4x +3x =7x =7

 $\Rightarrow x = 1$

So r = 4cm and R = 3cm

Surface area of a sphere $= 4\pi r^2$

Difference in total surface area = $4\pi r^2 - 4\pi R^2 = 4\pi (r^2 - R^2)$

$$4 \times \frac{22}{7} \times 7 = 88 \text{ cm}^2$$

70. Question

A hemispherical bowl of radius 9 cm contains a liquid. This liquid is to be filled into cylindrical small bottles of diameter 3 cm and height 4 cm. How many bottles will be needed to empty the bowl?



Thus, total 54 bottles are required.

71. Question

A cone and a hemisphere have equal bases and equal volumes. The ratio of their heights is

A. 1 : 2 B. 2 : 1 C. 4 : 1 D. $\sqrt{2}$: 1

Given that Radius of the hemisphere = Radius of cone

And Volume of hemisphere = Volume of cone

Volume of a hemisphere $=\frac{2}{3}\pi r^{3}$ Volume of a cone $=\frac{1}{3}\pi r^{2}h$ $\Rightarrow \frac{2}{3}\pi r^{3} = \frac{1}{3}\pi r^{2}h$ $\Rightarrow \frac{h}{r} = \frac{2}{1}$

72. Question

A cone, a hemisphere and a cylinder stand on equal bases and have the same height. The ratio of their volumes is

2.0

A.1:2:3

B.2:1:3

- C. 2:3:1
- D.3:2:1

Answer

Given that Radius of the hemisphere = Radius of cone = Radius of cylinder

And Height of the hemisphere = Height of cone = Height of cylinder

Volume of a hemisphere $=\frac{2}{2}\pi r^{3}$

Volume of a cone = $\frac{1}{2}\pi r^2 h$

Volume of a cylinder = $\pi r^2 h$

Ratio of their volumes = $\frac{1}{3}\pi r^2 h$: $\frac{2}{3}\pi r^3$: $\pi r^2 h$

=h: 2r: 3h = 1: 2: 3

73. Question

If the volume and the surface area of a sphere are numerically the same, then its radius is

A. 1 unit

B. 2 units

C. 3 units

D. 4 units

Volume of a sphere $=\frac{4}{3}\pi r^3$ Surface area of a sphere $=4\pi r^2$ Given that volume = surface area

$$\Rightarrow \frac{4}{3}\pi r^3 = 4\pi r^2$$

 \Rightarrow r = 3 units

74. Question

Which is false in case of a hollow cylinder?

A. Curved surface area of a hollow cylinder = $2\pi h(R + r)$.

B. Total surface area of a hollow cylinder = $2\pi (R + r)(h + R - r)$

- C. Inner curved surface area of a hollow cylinder = $2\pi h (R r)$
- D. Area of each end of a hollow cylinder = $\pi (R^2 r^2)$

Answer

Inner curved surface area of a hollow cylinder = $2\pi rh$

75. Question

Which is false?

- A. Volume of a hollow sphere $=\frac{4}{3}\pi (R^3 R^3)$
- B. Volume of a hemisphere $=\frac{2}{3}\pi R^3$.
- C. Total surface area of a hemisphere $= 3\pi R^2$.
- D. Curved surface area of a hemisphere $= \pi R^2$.

Answer

Curved surface area of a hemisphere = $2\pi r^2$

76. Question

For a right circular cylinder of base radius = 7 cm and height = 14 cm, which is false?

A. Curved surface area = 616 cm^2 .

- B. Total surface area $= 924 \text{ cm}^2$.
- C. Volume = 2156 cm^3 .
- D. Total area of the end faces $= 154 \text{ cm}^2$.

A) Curved surface area of a cylinder = $2\pi rh$

$$\Rightarrow 2 \times \frac{22}{7}(7) \times 14 = 616 \text{ cm}^2$$

B) Total surface area of a cylinder = $2\pi r(r + h)$

$$\Rightarrow 2 \times \frac{22}{7}(7) \times (7 + 14) = 924 \text{ cm}^2$$

C) Volume of a cylinder = $\pi r^2 h$

$$\Rightarrow \frac{22}{7}(7^2) \times 14 = 2156 \text{ cm}^3$$

D) Total area of the end faces = $2 \times \pi^2$ {Because there are two circular faces}

$$= 2 \times \frac{22}{7} \times 49 = 308 \text{ cm}^2$$

77. Question

Which is false?

A metal pipe is 63 cm long. Its inner diameter is 4 cm and the outer diameter is 4.4 cm. Then,

A. its inner curved surface area = 792 cm²

- B. its outer curved surface area = 871.2 cm²
- C. surface area of each end = 2.64 cm^2
- D. its total surface area = 1665.84 cm^2

Answer

A) Inner curved surface area = $2\pi rh$

$$\Rightarrow 2 \times \frac{22}{7} (2) \times 63 = 792 \text{ cm}^2$$

B) Outer curved surface area = $2\pi Rh$

$$\Rightarrow 2 \times \frac{22}{7} (2.2) \times 63 = 871.2 \text{ cm}^2$$

C) Surface area of the end face = $\pi(R^2 - r^2)$ {Because there are two circular faces}

$$= 2 \times \frac{22}{7} \times (2.2^2 - 2^2) = 2.64 \text{ cm}^2$$

D) R = 2.2 cm, r = 2 cm and h = 63 cm

Total surface area of a hollow cylinder = $2\pi (R + r)(h + R - r)$.

$$= 2 \times \frac{22}{7} \times 4.2 \times 63.2 = 1668.48 \text{ cm}^2$$

78. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Please select the correct answer.

Assertion (A)	Reason (R)
The base radius of a cone is 7 cm and its slant height is 25 cm. The volume of the cone is 1232 cm ³ .	The volume of a right circular cone of base radius r and height f_{1} is $\frac{1}{3}\pi r^{2}h$.

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) and Reason (R) are true but Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

Answer

Slant height $l = \sqrt{h^2 + r^2}$

Here, r=7cm and I=25cm

$$h = \sqrt{25^2 - 7^2} = \sqrt{576} = 24cm$$

Volume of a cone = $\frac{1}{3}\pi r^2 h$

$$\Rightarrow \frac{1}{3} \times \frac{22}{7} \times (7)^2 \times 24 = 1232 \text{cm}^2$$

Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

79. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Please select the correct answer.

Assertion (A)	Reason (R)
The surface area of a sphere is 2464 cm ² . Its volume is $11498\frac{2}{3}$ cm ³ .	The volume of a sphere of radius r is $\frac{4}{3}\pi r^3$.
$\left(\pi = \frac{22}{7}\right).$	con

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) and Reason (R) are true but Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

Answer

Surface area of a sphere $= 4\pi r$

Given Surface area = 2464 cm^2

$$\Rightarrow 4 \times \frac{22}{7} \times r^2 = 2464$$

$$\Rightarrow r^2 = \frac{2464 \times 7}{88} = 196$$

 \Rightarrow r = 14cm

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume
$$=\frac{4}{3}\pi(14)^3 = \frac{4}{3} \times \frac{22}{7} \times (14)^3 = 11498\frac{2}{3}$$
 cm³

Both Assertion (A) and Reason (R) are true but Reason (R) is not a correct explanation of Assertion (A).

80. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Please select the correct answer.

Assertion (A)	Reason (R)
The outer and inner radii of a hollow	The volume of a hollow
cylinder 2 m 10 cm long are 5 cm	cylinder of length h ,
and 3 cm respectively. If it is made	external radius R and
up of copper, then volume of copper	internal radius r is given
in it is 10560 cm ³ .	by $V = \pi h (R^2 - r^2)$.

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) and Reason (R) are true but Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

Answer

The volume of a hollow cylinder with external and internal radii R and r respectively and height h = $\pi (R^2 - r^2)h$

 $= \pi(5^2 - 3^2) \times 210$

$$=\frac{22}{7}\times 16\times 210$$

Thus, the volume is 10560cm³

Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

81. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Please select the correct answer.

Assertion (A)	Reason (R)
If the radius of a sphere is doubled then the ratio of the volume of the first sphere to that of the second is 1 : 8.	A cone and a hemisphere have equal bases and equal volumes. The ratio of their heights is 1 : 2.

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) and Reason (R) are true but Reason (R) is not a correct explanation of Assertion (A).

C

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume
$$=\frac{4}{3}\pi(2r)^3 = \frac{32}{3}\pi r^3$$

Ratio = 1:8

Reason is wrong. Assertion (A) is true and Reason (R) is false.

82. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Please select the correct answer.

Assertion (A)	Reason (R)
The curved surface area of a cone is 550 cm ² and its diameter is 14 cm. Then, its slant height is 25 cm.	The curved surface area of a cone having base radius <i>r</i> and slant height <i>i</i> is <i>πrl</i> .

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) and Reason (R) are true but Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

Answer

Curved surface area of a cone = πrl

$$\Rightarrow \frac{22}{7} \times 7 \times l = 550 \text{cm}^2$$

⇒ I=25 cm

Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

83. Question

A right circular cylinder just encloses a sphere of radius r (as shown in the figure). Then, the surface area of the sphere is equal to the curved surface area of the cylinder.



Answer

True

Curved surface area of a sphere = $4\pi r$

Radius of cylinder = r + r = 2r

Curved surface area of a cylinder = $2\pi rh$ = $2\pi \times r \times 2r = 4\pi r^2$

84. Question

The largest possible right circular cone is cut out of a cube of edge r cm. The volume of the cone is

$$\frac{1}{12}\pi r^3.$$

Answer

True

The dimensions of the cone arediameter = r ; radius = r/2 height = rVolume of a cone = $\frac{1}{2}\pi r^2 h$

$$= \frac{1}{3}\pi(\frac{r}{2})^2 \times r = \frac{1}{12}\pi r^3$$

85. Question

If a sphere is inscribed in a cube, then the ratio of the volume of the cube to the volume of the sphere will be 6 : π .

Answer

True

Let the radius of sphere be r so the edge of cube = 2r

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume of a cube = $(2r)^3$

Ratio of their volumes = $8r^3: \frac{4}{3}\pi r^3 = 6: \pi$

86. Question

If the length of diagonal of a cube is $6\sqrt{3}$ cm, then the length of each edge of the cube is 3 cm.

Answer

False

Diagonal of the cube = $side\sqrt{3}$

Length of longest rod = $6\sqrt{3}$ cm

Side = 6 cm

Formative Assessment (Unit Test)

1. Question

The radii of two cylinders are in the ratio of 2 : 3 and their heights are in the ratio of 5 : 3. Then, the ratio of their volumes is

A. 10 : 17

B. 20 : 27

C. 17:27

D. 20:37

Answer

Let the radii be 2x and 3x respectively and heights be 5y and 3y respectively.

Volume of a cylinder = $\pi r^2 h$

 $\Rightarrow \text{Ratio of their Volumes} = \frac{\pi r^2 h}{\pi R^2 H} = \frac{2x^2 \times 5y}{3x^2 \times 3y}$

Thus, the ratio of two cylinders $=\frac{20}{27}$

2. Question

The total surface area of a cone whose radius is $\frac{r}{2}$ and slant height 2/ is

- A. $2\pi r (l + r)$
- B. $\pi r \left(l + \frac{r}{4} \right)$
- C. $\pi r (l + r)$
- D. 2πrl

Answer

Total surface area of a cone = $\pi r(r + l)$

$$=\pi \frac{r}{2}\left(\frac{r}{2}+2l\right)$$

 $=\pi r(\frac{r}{4}+l)$

3. Question

A cone is 8.4 cm high and the radius of its base is 2.1 cm. It is melted and recast into a sphere. The radius of the sphere is

A. 1.6 cm

B. 2.1 cm

C. 2.4 cm

D. 4.2 cm

Answer

Volume of a cone = $\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi (2.1)^2 \times 8.4$

 $= 12.348\pi \text{ cm}^3$

On recasting a cone into sphere, the volume will remain same

Volume of a sphere $=\frac{4}{3}\pi r^3$

Volume of sphere =12.348 π cm³

$$\Rightarrow \frac{4}{3}\pi r^3 = 12.348\pi$$
$$\Rightarrow r^3 = 12.348 \times \frac{3}{4} = 9.261$$

 \Rightarrow r = 2.1cm

4. Question

The radius of a hemispherical balloon increases from 6 cm to 12 cm as air is being pumped into it. The ratio of the surface areas of the balloon in the two cases is

A.1:4

B.1:3

C. 2:3

D. 2:1

Answer

Surface area of a hemisphere = $2\pi r^2$

Radii are 6cm and 12 cm respectively

Ratio of surface areas $=\frac{2\pi r^2}{2\pi R^2}=\frac{6^2}{12^2}=\frac{1}{4}$

5. Question

A copper sphere of diameter 6 cm is melted and drawn into 36 cm long wire of uniform circular crosssection. Then, its radius is

çÓ

A. 2 cm

B. 1.5 cm

C. 1.2 cm

D. 1 cm

Answer

Radius of the sphere = 3 cm

Volume of a sphere $=\frac{4}{3}\pi r^3 = \frac{4}{3}\pi (3)^3 = 36\pi \text{ cm}^3$

On recasting a sphere into cylinder wire, the volume will remain same

Volume of a cylinder = $\pi r^2 h$

 $\Rightarrow \pi(r)^2 36 = 36\pi$

 \Rightarrow r = 1cm

6. Question

Find the lateral surface area and the total surface area of a cube of side 8 cm.

Answer

Total surface area of a cube = $6(side)^2$ \Rightarrow Total surface area = $6(8)^2 cm^2$ = $384 cm^2$ Lateral surface area of a cube = $4(side)^2$ \Rightarrow Total surface area = $4(8)^2 cm^2$ = $256 cm^2$

7. Question

Find the lateral surface area and the total surface area of a cuboid of dimensions 40 cm \times 30 cm \times 20 cm.

Answer

Total surface area of a cuboid = 2[(Length ×Breadth) + (Breadth ×Height) + (Height ×Length)]

Total surface area = $2[(40 \times 30) + (30 \times 20) + (20 \times 40)]$ cm² = 2(1200 + 600 + 800) cm²

 $= 2(2600) \text{ cm}^2 = 5200 \text{ cm}^2$

Lateral surface area of a cuboid = 2(Length +Breadth) ×Height

Lateral surface area = $2(40+30) \times 20 \text{ cm}^2 = 140 \times 20 \text{ cm}^2$

 $= 2800 \text{ cm}^2$

8. Question

The total surface area of a cylinder is 462 cm^2 and its curved surface area is one-third of its total surface area. Find the volume of the cylinder.

Answer

Total surface area of a cylinder = $2\pi r(r + h)$

Curved surface area of a cylinder = $2\pi rh$

$$\Rightarrow \frac{2\pi rh}{2\pi r(r+h)} = \frac{1}{3}$$

 \Rightarrow 3h=r+h \Rightarrow 2h=r

Given that total surface area = 462 cm^2

$$\Rightarrow 2 \times \frac{22}{7} \times \frac{3}{2} r^2 = 462$$

$$\Rightarrow$$
 r² = 7× 7

So, r = 7 cm, h = 3.5 cm

Volume of a cylinder = $\pi r^2 h$

$$\Rightarrow \frac{22}{7} \times 49 \times 3.5 = 539 \,\mathrm{cm}^3$$

9. Question

The length and breadth of a room are in a ratio 3 : 2. The cost of carpeting the room at Rs 25 per m² is Rs 1350 and the cost of papering the four walls at Rs 15 per m² is Rs 2580. If one door and two windows occupy $8m^2$, find the dimensions of the room.

Answer

Area of the floor = $\frac{\text{Cost of carpeting}}{\text{rate of carpeting}} = \frac{1350}{25} = 54 \text{ m}^2$

Given that length and breadth are in ratio 3:2, so I = 3x and b = 2x

$$\Rightarrow$$
 I= 9 m and b = 6 m

Lateral surface area of a cuboid = 2(Length +Breadth) ×Height

Lateral surface area = $\frac{2580}{15} = 172 \text{ m}^2$

Adding door and window, Lateral surface area = 180 m^2

$$\Rightarrow 2(l+b)h = 2(15 \times h) = 180$$

10. Question

If the radius of a sphere is increased by 10%, prove that its volume will be increased by 33.1%.

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Let the radius be 'r'Increased Radius = 1.1r

Volume = $\frac{4}{3}\pi(1.1r)^3 = \frac{4\times1.331}{3}\pi r^3$

Change in volume = $\frac{\frac{4}{3} \times 1.331 \text{m}^3 - \frac{4}{3} \text{m}^3}{\frac{4}{3} \text{m}^3} \times 100\% = \frac{0.331}{1} \times 100\% = 33.1\%$

11. Question

The surface area of a sphere of radius 5 cm is five times the area of the curved surface of a cone of radius 4 cm. Find the height and volume of the cone. $\left(\text{Take } \pi = \frac{22}{7} \right)$

Answer

Curved surface area of a sphere $= 4\pi r^2$

Curved Surface area of a cone $= \pi r l$

Given that $\Rightarrow 4\pi r^2 = 5(\pi r l)$

$$\Rightarrow l = \frac{4 \times 25}{5 \times 4} = 5 cm$$

I= 5 cm and r= 4 cm

h =
$$\sqrt{5^2 - 4^2} = \sqrt{9} = 3$$
cm
Volume = $\frac{1}{3} \times \frac{22}{7} \times 4^2 \times 3 = 50.3$ cm³

12. Question

A rectangular tank measuring $5m \times 4.5m \times 2.1$ m is dug in the centre of the field measuring 13.5m \times 2.5 m. The earth dug out is spread over the remaining portion of the field. How much is the level of the field raised?

Answer

Volume = $I \times b \times h$

Volume = $5 \times 4.5 \times 2.1 = 47.25 \text{ m}^3$

Area over which it is spread = $13.5 \times 25 - 5 \times 4.5 = 33.75 - 220 = 11.75$ mRise in level = $\frac{47.25}{11.75} = 4.2$

m

13. Question

A joker's cap is in the form of a right circular cone of base radius 7 cm and height 24 cm. Find the area of the sheet required to make 10 such caps.

Answer

Curved surface area of a cone = πr

where $l = \sqrt{h^2 + r^2}$

Here, r=7cm and h=24cm

$$l = \sqrt{24^2 + 7^2} = \sqrt{625} = 25 \text{cm}$$

$$\Rightarrow \frac{22}{7} \times 7 \times 25 = 550 \text{ cm}$$

Area of 10 such caps = 5500 cm^2

14. Question

The volume of a right circular cone is 9856 cm^3 . If the diameter of its base is 28 cm, find the height of the cone.

Answer

Volume of a cone = $\frac{1}{3}\pi r^2 h$

Given volume = 9856 cm^3

Radius of cone = 14 cm

$$\Rightarrow \frac{1}{3}\pi(14)^2 \times h = \frac{22}{21} \times 196 \times h = 9856 \text{cm}^3$$
$$\Rightarrow h = 48 \text{ cm}$$

15. Question

Into a circular drum of radius 4.2 m and height 3.5 m, how many full bags of wheat can be emptied if the space required for wheat in each bag is 2.1 m^3 ?

Answer

Volume of a cylinder = $\pi r^2 h$

Volume of the cylinder = $\pi(4.2)^2 \times 3.5$

Number of bags = $\frac{\text{Volume of the cylinder}}{\text{Volume of the wheat bags}} = \frac{\pi (4.2)^2 \times 3.5}{2.1} = 92$

16. Question

A well with 10 m inside diameter is dug 14 m deep. Earth taken out of it is spread all around to a width of 5 m to form an embankment. Find the height of the embankment.

Answer

Volume of a cylinder = $\pi r^2 h$

Radius of well = 5m, Height of well = 14m

Volume of the well = $\pi(5)^2 \times 14 = \frac{22}{7} \times 25 \times 14 = 1100 \text{m}^2$

For embankment, radius = 5+5=10 m and let height be h m

Volume of well = Volume of embankment

$$\Rightarrow \pi[(10)^2 - (5)^2] \times h = \frac{22}{7} \times 75 \times h = 1100$$

⇒ h = 4.67 m

17. Question

How many metres of cloth 5 m wide will be required to make a conical tent, the radius of whose base is 7 m and whose height is 24 m?

Answer

Curved surface area of a cone = πrl

where
$$l = \sqrt{h^2 + r^2}$$

Here, r=7m and h=24m

$$l = \sqrt{24^2 + 7^2} = \sqrt{625} = 25m$$

 $\Rightarrow \frac{1}{7} \times 7 \times 25 = 550 \text{m}^2$ The cloth required = $\frac{550}{5} = 110 \text{m}$

18. Question

The volume of a solid cylinder is 1584 cm^3 and its height is 14 cm. Find its total surface area.

Answer

Volume of a cylinder = $\pi r^2 h$, Given volume = 1584 cm³

$$\Rightarrow \frac{22}{7} \times r^2 \times 14 = 1584 \text{ cm}^3$$

$$\Rightarrow$$
 r² = 36 \Rightarrow r =6 cm

Total surface area of a cylinder = $\pi r(r + h)$

$$\Rightarrow \frac{22}{7} \times 6 \times (6+14) = 754.29 \text{ cm}^2$$

19. Question

The volume of two spheres are in the ratio 64 : 27. Find the difference of their surface areas if the sum of their radii is 7 cm.

Answer

Volume of a sphere $=\frac{4}{3}\pi r^3$

Given Ratio of volumes of two spheres $=\frac{6}{2}$

$$\Rightarrow \frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi R^3} = \frac{r^3}{R^3} = \frac{64}{27}$$
$$\Rightarrow \frac{r}{R} = \frac{4}{2}$$

So, r = 4x and R = 3x

Also given that the sum of radii = 7

$$\Rightarrow r + R = 4x + 3x = 7x = 7$$

 $\Rightarrow x = 1$

So, r = 4cm and R = 3cm

Surface area of a sphere $= 4\pi r^2$

Difference in total surface area = $4\pi r^2 - 4\pi R^2 = 4\pi (r^2 - R^2)$

$$4 \times \frac{22}{7} \times 7 = 88 \text{ cm}^2$$

20. Question

The radius and height of a right circular cone are in the ratio 4 : 3. and its volume is 2156 cm³. Find the curved surface area of the cone.

Answer

Since the radius and height of a cone is 4:3 so let radius = 4x and height = 3x

Volume of a cone = $\frac{1}{3}\pi r^2 h$, Given volume = 2156 cm³.

$$\Rightarrow \frac{1}{3} \times \frac{22}{7} \times (4x)^2 \times 3x = 2156 \text{ cm}^3$$
$$\Rightarrow x^3 = \frac{343}{8} \Rightarrow x = \frac{7}{2}$$

So , r = 14 cm and height = 10.5 cm

slant height $l = \sqrt{h^2 + r^2}$

Here, r=14 cm and h=10.5 cm

$$l = \sqrt{14^2 + 10.5^2} = \sqrt{306.25} = 17.5$$
 cm

Curved surface area of a cone = πr

$$\Rightarrow \frac{22}{7} \times 14 \times 17.5 = 770 \text{ cm}^2$$

21. Question

The radius of the base of a cone is 14 cm and its height is 24 cm. Find the volume, curved surface area and the total surface area of the cone.

2.00

Answer

Curved surface area of a cone = πrl

where
$$l = \sqrt{h^2 + r^2}$$

Here, r=14cm and h=24cm

$$l = \sqrt{24^2 + 14^2} = \sqrt{772} = 27.8 \text{cm}$$
$$\Rightarrow \frac{22}{7} \times 14 \times 27.8 = 1223 \text{ cm}^2$$

Total surface area of a cone = $\pi r(r + l)$

$$\Rightarrow \frac{22}{7} \times 14 \times (14 + 27.8) = 1839 \,\mathrm{cm}^2$$

Volume of a cone = $\frac{1}{3}\pi r^2 h$

$$\Rightarrow \frac{1}{3} \times \frac{22}{7} \times (14)^2 \times 24 = 4928 \text{ cm}^3$$

22. Question

Two cylindrical vessels are filled with oil. Their radii are 15 cm and 10 cm respectively and their heights are 25 cm and 18 cm respectively. Find the radius of the cylindrical vessel 33 cm in height which will just contain the oil of the two given vessels.

Answer

Volume of a cylinder = $\pi r^2 h$

Volume of first vessel = $\frac{22}{7} \times 15^2 \times 25 = 17678.57 \text{ cm}^3$

Volume of second vessel = $\frac{22}{7} \times 10^2 \times 18 = 5657.14 \text{ cm}^3$

The volume of the third vessel = volume of first vessel + volume of second vessel

$$\Rightarrow \frac{22}{7} \times r^2 \times 33 = 17678.57 + 5657.14$$

 \Rightarrow r² = 225 \Rightarrow r = 15 cm

23. Question

The ratio of the curved surface area and the total surface area of a circular cylinder is 1:2 and the total surface area is 616 cm². Find its volume.

Answer

Total surface area of a cylinder = $2\pi r(r + h)$

Curved surface area of a cylinder = $2\pi rh$

$$\Rightarrow \frac{2\pi rh}{2\pi r(r+h)} = \frac{1}{2}$$

$$\Rightarrow$$
 2h=r + h

 \Rightarrow h=r

Given that total surface area = 616 cm^2

$$\Rightarrow 2 \times \frac{22}{7} \times 2r^2 = 616$$

 \Rightarrow r² = 7× 7

So, r = h = 7 cm

Volume of a cylinder = $\pi r^2 h$

$$\Rightarrow \frac{22}{7} \times 49 \times 7 = 1078 \text{ cm}^3$$