

Linear Inequations

EXERCISE - 4.1

Q1. Solve the inequation $3x - 11 < 3$. where $x \in \{1, 2, 3, \dots, 10\}$
also represent the solution on a number line.

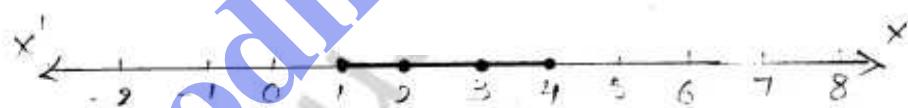
Sol.

$$\begin{aligned}3x - 11 &< 3 \\ \Rightarrow 3x &< 3 + 11 \\ \Rightarrow 3x &< 14 \\ \Rightarrow x &< \frac{14}{3}\end{aligned}$$

But $x \in \{1, 2, 3, \dots, 10\}$

\therefore Solution set is $\{1, 2, 3, 4\}$

Solution set on number Line



Sol.

$$\begin{aligned}2(x-3) &< 1 \\ \Rightarrow x-3 &< \frac{1}{2} \\ \Rightarrow x &< \frac{1}{2} + 3 \\ \Rightarrow x &< 3\frac{1}{2}\end{aligned}$$

But $x \in \{1, 2, 3, \dots, 10\}$

\therefore Solution set = $\{1, 2, 3\}$

Q3. solve $5 - 4x > 2 - 3x$, $x \in \mathbb{W}$. Also represent its solution on the number line.

Sol.

$$5 - 4x > 2 - 3x$$

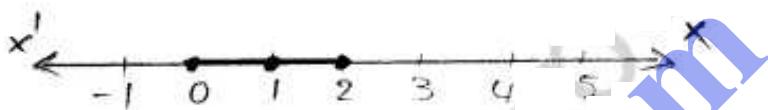
$$\Rightarrow -4x + 3x > 2 - 5$$

$$\Rightarrow -x > -3$$

$$\Rightarrow x < 3 \quad (\because x \in \mathbb{W})$$

\therefore solution set $\{0, 1, 2\}$

Solution set on number line:



Q4. List the solution set of $30 - 4(2x - 1) < 30$, given that x is a positive integer.

Sol.

$$30 - 4(2x - 1) < 30$$

$$\Rightarrow 30 - 8x + 4 < 30$$

$$\Rightarrow -8x < 30 - 30 - 4$$

$$\Rightarrow -8x < -4$$

$$\Rightarrow x > \frac{-4}{-8}$$

$$\Rightarrow x > \frac{1}{2}$$

$\therefore x$ is a positive integer

$$\therefore x = \{1, 2, 3, 4, \dots\}$$

Q5. Solve $2(x-2) < 3x - 2$, $x \in \{-3, -2, -1, 0, 1, 2, 3\}$

Sol.

$$2(x-2) < 3x - 2$$

$$\Rightarrow 2x - 4 < 3x - 2$$

$$\Rightarrow -x < 2$$

$$\Rightarrow x > -2$$

$$\therefore \text{solution set} = \{-1, 0, 1, 2, 3\}$$

Q6. If x is a negative integer, find the solution set of $\frac{2}{3} + \frac{1}{3}(x+1) > 0$

$$\text{sol. } \frac{2}{3} + \frac{1}{3}x + \frac{1}{3} > 0$$

$$\Rightarrow \frac{1}{3}x + 1 > 0$$

$$\Rightarrow \frac{1}{3}x > -1$$

$$\Rightarrow x > -1 \times \frac{3}{1}$$

$$\Rightarrow x > -3$$

$\therefore x$ is a negative integer

$$\therefore \text{solution set} = \{-2, -1\}$$

Q7. solve $\frac{2x-3}{4} > \frac{1}{2}$, $x \in \{0, 1, 2, \dots, 8\}$

$$\text{sol. } \frac{2x-3}{4} > \frac{1}{2}$$

$$\Rightarrow 2x-3 > \frac{4}{2}$$

$$\Rightarrow 2x > 5$$

$$\Rightarrow x > \frac{5}{2}$$

$$\therefore x \in \{0, 1, 2, \dots, 8\}$$

$$\therefore \text{solution set} = \{3, 4, 5, 6, 7, 8\}$$

Q8. solve $x-3(2+x) > 2(3x-1)$, $x \in \{-3, -2, -1, 0, 1, 2\}$
also represent its solution on the number line.

$$\text{sol. } x-3(2+x) > 2(3x-1)$$

$$\Rightarrow x-6-3x > 6x-2$$

$$\Rightarrow x-3x-6x > -2+6$$

$$\Rightarrow -8x > 4$$

$$\Rightarrow x < -\frac{1}{2}$$

$$\therefore x \in \{-3, -2, -1, 0, 1, 2\}$$

$$\text{solution set} = \{-3, -2, -1\}$$

Solution set on number line:



Q9. Given $x \in \{1, 2, 3, 4, 5, 6, 7, 9\}$, solve $x-3 < 2x-1$

$$x-3 < 2x-1$$

$$\Rightarrow x-2x < -1+3$$

$$\Rightarrow -x < 2$$

$$\Rightarrow x > -2$$

$$\therefore \text{But } x \in \{1, 2, 3, 4, 5, 6, 7, 9\}$$

$$\therefore \text{solution set} = \{1, 2, 3, 4, 5, 6, 7, 9\}$$

Q10. Given $A = \{x : x \in \mathbb{I}, -4 \leq x \leq 4\}$, solve $2x-3 < 3$
where x has the domain A . Graph the solution set on the number line.

$$2x-3 < 3$$

$$\Rightarrow 2x < 3+3$$

$$\Rightarrow x < 3$$

$$\text{But } x \text{ has the domain } A = \{x : x \in \mathbb{I}, -4 \leq x \leq 4\}$$

$$\therefore \text{solution set} = \{-4, -3, -2, -1, 0, 1, 2, 3\}$$

solution set on number line:



Q11. List the solution set of the inequation

$$\frac{1}{2} + 8x > 5x - \frac{3}{2} \quad x \in \mathbb{Z}$$

Sol.

$$\frac{1}{2} + 8x > 5x - \frac{3}{2}$$

$$\Rightarrow 8x - 5x > -\frac{3}{2} - \frac{1}{2}$$

$$\Rightarrow 3x > -2$$

$$\Rightarrow x > -\frac{2}{3}$$

$$\therefore x \in \mathbb{Z}$$

$$\therefore \text{solution set} = \{0, 1, 2, 3, \dots\}$$

Q12. list the solution set of $\frac{11-2x}{5} \geq \frac{9-3x}{8} + \frac{3}{4} \quad x \in \mathbb{N}$

Sol.

$$\frac{11-2x}{5} \geq \frac{9-3x}{8} + \frac{3}{4}$$

$$\Rightarrow 88 - 16x \geq 45 - 15x + 30$$

$$\therefore \text{L.C.M of } 8, 5, 4 = 40 \}$$

$$\Rightarrow -16x + 15x \geq 45 + 30 - 88$$

$$\Rightarrow -x \geq -13$$

$$\Rightarrow x \leq 13$$

$$\therefore x \in \mathbb{N}$$

$$\therefore \text{solution set} = \{1, 2, 3, 4, 5, \dots, 13\}$$

Q13. find the values of x , which satisfy the inequation

$$-2 \leq \frac{1}{2} - \frac{2x}{3} \leq 1\frac{5}{6} \quad x \in \mathbb{N} \quad \text{Graph the solution set on the number line.}$$

Sol.

$$-2 \leq \frac{1}{2} - \frac{2x}{3} \leq 1\frac{5}{6}$$

$$\Rightarrow -2 \leq \frac{1}{2} - \frac{2x}{3} \leq \frac{11}{6}$$

$$\Rightarrow -12 \leq 3 - 4x \leq 22 \quad \left\{ \because \text{LCM of } 2, 3, 6 = 6 \right\}$$

$$-12 \leq 3 - 4x \text{ and } 3 - 4x \leq 22$$

$$\Rightarrow 4x \leq 3 + 12 \text{ and } -4x \leq 22 - 3$$

$$\Rightarrow 4x \leq 15 \text{ and } -4x \leq 19$$

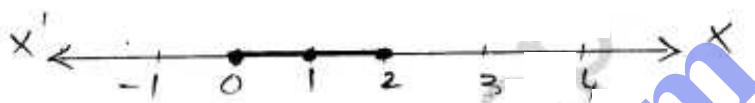
$$\Rightarrow x \leq \frac{15}{4} \text{ and } x \geq -\frac{19}{4}$$

$$\Rightarrow -\frac{19}{4} \leq x \leq \frac{15}{4}$$

$\therefore x \in \mathbb{N}$

$$\therefore \text{solution set} = \{1, 2, 3\}$$

solution set on number Line



Q14. If $x \in \mathbb{W}$, find the solution set of $\frac{3}{5}x - \frac{2x-1}{3} > 1$.
Also graph the solution set on the number Line, if possible.

Sol.

$$\frac{3}{5}x - \frac{2x-1}{3} > 1$$

$$\Rightarrow 9x - (10x - 5) > 15 \quad \left\{ \because \text{LCM of } 5, 3 = 15 \right\}$$

$$\Rightarrow 9x - 10x + 5 > 15$$

$$\Rightarrow -x > 10$$

$$\Rightarrow x < -10$$

But $x \in \mathbb{W}$

$$\frac{x}{2} - \frac{4}{3} < \frac{1}{6}$$

$$\text{Solution set} = \emptyset$$

Hence it can't be represented on number Line.

Q15.

Solve :

- (i) $\frac{x}{2} + 5 \leq \frac{x}{3} + 6$, where x is a positive odd integer
- (ii) $\frac{2x+3}{3} \geq \frac{3x-1}{4}$, where x is positive even integer.

sol:

$$(i) \quad \frac{x}{2} + 5 \leq \frac{x}{3} + 6$$

$$\Rightarrow \frac{x}{2} - \frac{x}{3} \leq 6 - 5$$

$$\Rightarrow \frac{3x - 2x}{6} \leq 1$$

$$\Rightarrow \frac{x}{6} \leq 1$$

$$\Rightarrow x \leq 6$$

$\therefore x$ is a positive odd integer

$$\therefore x = \{1, 3, 5\}$$

$$(ii) \quad \frac{2x+3}{3} > \frac{3x-1}{4}$$

$$\Rightarrow \frac{2x}{3} + \frac{3}{3} > \frac{3x}{4} - \frac{1}{4}$$

$$\Rightarrow \frac{2x}{3} - \frac{3x}{4} > -\frac{1}{4} - 1$$

$$\Rightarrow \frac{8x - 9x}{12} > -\frac{5}{4}$$

$$\Rightarrow \frac{-x}{12} > -\frac{5}{4}$$

$$\Rightarrow \frac{x}{12} \leq \frac{5}{4}$$

$$\Rightarrow x \leq \frac{5}{4} \times 12$$

$$\Rightarrow x \leq 15$$

$\therefore x$ is positive even integer.

$$\therefore x = \{2, 4, 6, 8, 10, 12, 14\}$$

Q16. Given that $x \in \mathbb{I}$, solve the inequation and graph the solution on the number line : $3 \geq \frac{x-4}{2} + \frac{x}{3} \geq 2$

Sol.

$$3 \geq \frac{x-4}{2} + \frac{x}{3} \text{ and } \frac{x-4}{2} + \frac{x}{3} \geq 2$$

$$3 \geq \frac{3x - 12 + 2x}{6} \text{ and } \frac{3x - 12 + 2x}{6} \geq 2$$

$$\Rightarrow 3 \geq \frac{5x - 12}{6} \text{ and } \frac{5x - 12}{6} \geq 2$$

$$\Rightarrow 5x - 12 \leq 18 \text{ and } 5x - 12 \geq 12$$

$$\Rightarrow 5x \leq 30 \text{ and } 5x \geq 24$$

$$\Rightarrow x \leq 6 \text{ and } x \geq \frac{24}{5} \Rightarrow x \geq 4\frac{4}{5}$$

$$\therefore x = \{5, 6\}$$

Solution set on number line



Q17. Given $x \in \{1, 2, 3, 4, 5, 6, 7, 9\}$, find the values of x which $-3 < 2x-1 < x+4$.

Sol.

$$-3 < 2x-1 \text{ and } 2x-1 < x+4$$

$$\Rightarrow -2x < -1+3 \text{ and } 2x-x < 4+1$$

$$\Rightarrow -2x < 2 \text{ and } x < 5$$

$$\Rightarrow -x < 1$$

$$\Rightarrow x > -1$$

$$\therefore -1 < x < 5$$

$$\therefore x \in \{1, 2, 3, 4, 5, 6, 7, 9\}$$

$$\therefore \text{Solution set} = \{1, 2, 3, 4\}$$

Q18. Solve $1 \geq 15 - 7x > 2x - 27$, $x \in \mathbb{N}$

Sol. $1 \geq 15 - 7x > 2x - 27$

$$\Rightarrow 1 \geq 15 - 7x \text{ and } 15 - 7x > 2x - 27$$

$$\Rightarrow 7x \geq 15 - 1 \text{ and } -7x - 2x > -27 - 15$$

$$\Rightarrow 7x \geq 14 \text{ and } -9x > -42$$

$$\Rightarrow x \geq 2 \text{ and } -x > -\frac{42}{9}$$

$$\Rightarrow 2 \leq x \text{ and } -x > -\frac{14}{3}$$

$$x < \frac{14}{3}$$

$$\therefore 2 \leq x < \frac{14}{3}$$

But $x \in \mathbb{N}$

$$\therefore \text{solution set} = \{2, 3, 4\}$$

Q19. If $x \in \mathbb{Z}$, solve $2 + 4x < 2x - 5 \leq 3x$. Also represent its solution on the number line.

Sol.

$$2 + 4x < 2x - 5 \leq 3x$$

$$2 + 4x < 2x - 5 \text{ and } 2x - 5 \leq 3x$$

$$\Rightarrow 4x - 2x < -5 - 2 \text{ and } 2x - 3x \leq 5$$

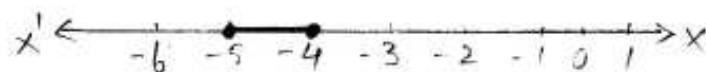
$$\Rightarrow 2x < -7 \text{ and } -x \leq 5$$

$$\Rightarrow x < -\frac{7}{2} \text{ and } x \geq -5$$

$$-5 \leq x < -\frac{7}{2}$$

$\therefore x \in \mathbb{Z}$

$$\therefore \text{solution set} = \{-5, -4\}$$



Q20. solve the inequation $12 + \frac{5}{6}x \leq 5 + 3x$, $x \in \mathbb{R}$. Represent the solution on a number line.

sol.

$$12 + \frac{5}{6}x \leq 5 + 3x$$

$$\Rightarrow 12 + \frac{11}{6}x \leq 5 + 3x$$

$$\Rightarrow 72 + 11x \leq 30 + 18x \quad \{ \text{Multiplying by 6} \}$$

$$\Rightarrow 11x - 18x \leq 30 - 72$$

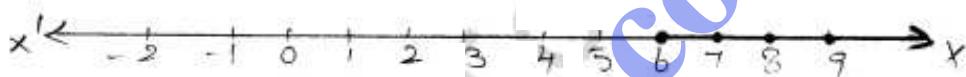
$$\Rightarrow -7x \leq -42$$

$$\Rightarrow x \geq 6$$

$$\therefore x \in \mathbb{R}$$

$$\text{solution set} = \{x; x \in \mathbb{R}, x \geq 6\}$$

solution set on number line



Q21. solve $\frac{4x-10}{3} \leq \frac{5x-7}{2}$, $x \in \mathbb{R}$ and represent the solution set on the number line.

sol.

$$\frac{4x-10}{3} \leq \frac{5x-7}{2}$$

$$\Rightarrow 8x - 20 \leq 15x - 21 \quad \{ \text{LCM of } 2, 3 = 6 \}$$

$$\Rightarrow 8x - 15x \leq -21 + 20$$

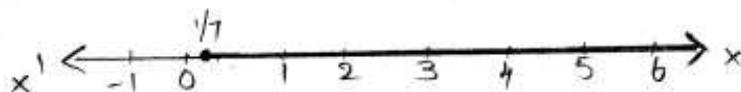
$$\Rightarrow -7x \leq -1$$

$$\Rightarrow x \geq \frac{1}{7}$$

$$\therefore x \in \mathbb{R}$$

$$\text{solution set} = \{x; x \in \mathbb{R}, x \geq \frac{1}{7}\}$$

solution set on Number Line



Q22. Solve $\frac{3x}{5} - \frac{2x-1}{3} > 1$, $x \in \mathbb{R}$ and represent the solution set on the number line.

Sol. $\frac{3x}{5} - \frac{2x-1}{3} > 1$

$$\Rightarrow 9x - (10x - 5) > 15$$

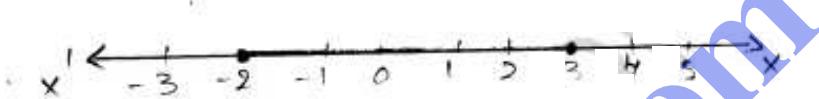
$$\Rightarrow -x > 15 - 5$$

$$\Rightarrow x < -10$$

$\therefore x \in \mathbb{R}$

$$\text{solution set} = \{x : x \in \mathbb{R}, x < -10\}$$

Solution set on the number line.



Q23. Solve the inequation $-3 \leq 3 - 2x \leq 9$, $x \in \mathbb{R}$. Represent the solution on a number line.

Sol. $-3 \leq 3 - 2x \leq 9$

$$-3 \leq 3 - 2x \quad \text{and} \quad 3 - 2x \leq 9$$

$$\Rightarrow 2x \leq 3 + 3 \quad \text{and} \quad -2x \leq 9 - 3$$

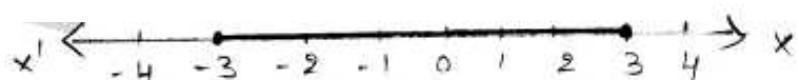
$$\Rightarrow 2x \leq 6 \quad \text{and} \quad -2x \leq 6$$

$$\Rightarrow x \leq 3 \quad \text{and} \quad -3 \leq x$$

$$\therefore -3 \leq x \leq 3$$

$$\text{solution set} = \{x : x \in \mathbb{R}, -3 \leq x \leq 3\}$$

Solution number line



Q24 Solve $2 \leq 2x - 3 \leq 5$, $x \in \mathbb{R}$ and mark it on number Line.

Sol. $2 \leq 2x - 3 \leq 5$

$$2 \leq 2x - 3 \leq 5$$

$$2 \leq 2x - 3 \text{ and } 2x - 3 \leq 5$$

$$2 + 3 \leq 2x \text{ and } 2x \leq 5 + 3$$

$$5 \leq 2x \text{ and } 2x \leq 8$$

$$\frac{5}{2} \leq x \text{ and } x \leq 4$$

$$\therefore \frac{5}{2} \leq x \leq 4$$

$$\therefore \text{solution set} = \{x; x \in \mathbb{R}, \frac{5}{2} \leq x \leq 4\}$$

solution set on number Line



Q25 Given that $x \in \mathbb{R}$, solve the following inequality and graph the solution on the number line:

$$-1 \leq 3 + 4x < 23$$

Sol. Given $-1 \leq 3 + 4x < 23, x \in \mathbb{R}$

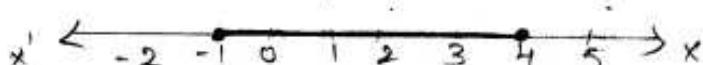
$$\Rightarrow -1 - 3 \leq 4x < 23 - 3$$

$$\Rightarrow -4 \leq 4x < 20$$

$$\Rightarrow -1 \leq x < 5$$

$$\therefore \text{The solution set} = \{x; x \in \mathbb{R}, -1 \leq x < 5\}$$

solution set on number Line



Q26. Solve the following inequation and represent the solution on the number line: $-2\frac{2}{3} \leq x + \frac{1}{3} < 3 + \frac{1}{3}$, $x \in \mathbb{R}$.

Sol.

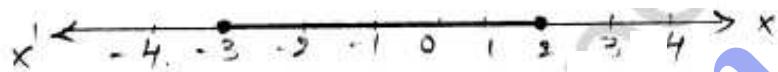
$$-2\frac{2}{3} \leq x + \frac{1}{3} < 3 + \frac{1}{3}$$

$$\Rightarrow -\frac{8}{3} \leq x + \frac{1}{3} < 3 + \frac{1}{3}$$

$$\Rightarrow -\frac{8}{3} - \frac{1}{3} \leq x < 3 + \frac{1}{3} - \frac{1}{3}$$

$$\Rightarrow -3 \leq x < 3$$

\therefore The solution set = $\{x : x \in \mathbb{R}, -3 \leq x < 3\}$
solution set on number line



Q27. Solve the inequation and represent the solution on the number line: $-\frac{2}{3} < -\frac{x}{3} + 1 \leq \frac{2}{3}$, $x \in \mathbb{R}$

Sol.

$$-\frac{2}{3} < -\frac{x}{3} + 1 \leq \frac{2}{3}$$

$$-\frac{2}{3} < -\frac{x}{3} + 1 \quad \text{and} \quad -\frac{x}{3} + 1 \leq \frac{2}{3}$$

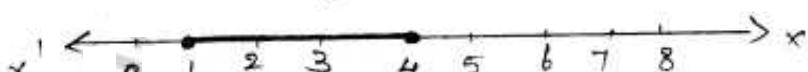
$$-2 < -x + 3 \quad \text{and} \quad -x + 3 \leq 2$$

$$x < 2 + 3 \quad \text{and} \quad -x \leq 2 - 3$$

$$x < 5 \quad \text{and} \quad 1 \leq x$$

$$\therefore 1 \leq x < 5$$

solution set = $\{x : x \in \mathbb{R}, 1 \leq x < 5\}$



Q28. Solve $\frac{2x+1}{2} + 2(3-x) \geq 7$, $x \in \mathbb{R}$. Also graph the solution set on number line.

Sol.

$$\frac{2x+1}{2} + 2(3-x) \geq 7$$

$$\Rightarrow \frac{2x+1}{2} + 6 - 2x \geq 7$$

$$\Rightarrow \frac{2x+1}{2} - 2x > 7 - 6$$

$$\Rightarrow \frac{2x+1-4x}{2} > 1$$

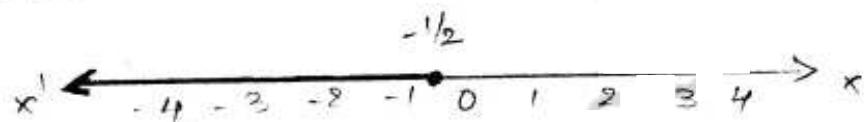
$$\Rightarrow -2x \geq 2 - 1$$

$$\Rightarrow -x \geq \frac{1}{2}$$

$$\Rightarrow x \leq -\frac{1}{2}$$

$$\text{solution set} = \left\{ x : x \in \mathbb{R}, x \leq -\frac{1}{2} \right\}$$

Solution on number Line



- Q29. find the range of values of x , which satisfy $-\frac{1}{3} \leq \frac{x}{2} - 1 \frac{1}{3} < \frac{1}{6}$, $x \in \mathbb{R}$. Graph the values of x on the real number line.

Sol.

$$-\frac{1}{3} \leq \frac{x}{2} - 1 \frac{1}{3} < \frac{1}{6}$$

$$\Rightarrow -\frac{1}{3} \leq \frac{x}{2} - 1 \frac{1}{3} \text{ and } \frac{x}{2} - 1 \frac{1}{3} < \frac{1}{6}$$

$$\Rightarrow -\frac{1}{3} \leq \frac{x}{2} - \frac{4}{3} \text{ and } \frac{x}{2} - \frac{4}{3} < \frac{1}{6}$$

$$\Rightarrow -2 \leq 3x - 8 \text{ and } 3x - 8 < 1$$

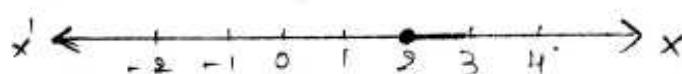
$$\Rightarrow -3x \leq -8 + 2 \text{ and } 3x < 1 + 8$$

$$\Rightarrow x \geq 2 \text{ and } x < 3$$

$$\therefore 2 \leq x < 3$$

$$\text{solution set} = \left\{ x : x \in \mathbb{R}, 2 \leq x < 3 \right\}$$

Solution set on number Line



Q30. Solve the inequation: $-2\frac{1}{2} + 2x \leq \frac{4x}{3} \leq \frac{4}{3} + 2x$, $x \in \mathbb{W}$
 Graph the solution set on the number line.

$$\text{Sol. } -2\frac{1}{2} + 2x \leq \frac{4x}{3} \leq \frac{4}{3} + 2x$$

$$-\frac{5}{2} + 2x \leq \frac{4x}{3} \leq \frac{4}{3} + 2x$$

$$-\frac{5}{2} + 2x \leq \frac{4x}{3} \quad \text{and} \quad \frac{4x}{3} \leq \frac{4}{3} + 2x$$

$$2x - \frac{4x}{3} \leq \frac{5}{2} \quad \text{and} \quad \frac{4x}{3} - 2x \leq \frac{4}{3}$$

$$12x - 8x \leq 15 \quad \text{and} \quad 4x - 6x \leq 4$$

$$4x \leq 15 \quad \text{and} \quad -2x \leq 4$$

$$x \leq \frac{15}{4} \quad \text{and} \quad x \geq -2$$

$$\therefore -2 \leq x \leq \frac{15}{4}$$

$$\text{Solution set} = \{x : x \in \mathbb{W}, x \leq 3\}$$

solution set on number line



Q31. If $x \in \mathbb{I}$, A is the solution set of $2(x-1) < 3x-1$ and B is the solution set of $4x-3 \leq 8+x$. find $A \cap B$.

$$2(x-1) < 3x-1$$

$$2x-2 < 3x-1$$

$$\leftarrow x < 1 \Rightarrow x > -1$$

$$\therefore \text{solution set of } A = \{0, 1, 2, 3, \dots\}$$

$$4x-3 \leq 8+x$$

$$3x \leq 11 \Rightarrow x \leq \frac{11}{3}$$

$$\text{solution set of } B = \{3, 2, 1, 0, -1, \dots\}$$

$$\therefore A \cap B = \{0, 1, 2, 3\}$$

Q32. If $x \in N$, P is the solution set of $5x-2 > 3x+4$ and Q is the solution set of $3x+1 \geq 19-x$, find $P \cap Q$.

Sol.

$$\begin{aligned} 5x-2 &> 3x+4 & 3x+1 &\geq 19-x \\ 2x &> 6 & 4x &\geq 18 \\ x &> 3 & x &\geq \frac{9}{2} \end{aligned}$$

Solution set $P = \{4, 5, 6, 7, \dots\}$ Solution set $Q = \{5, 6, 7, 8, \dots\}$
 $\therefore P \cap Q = \{5, 6, 7, 8, \dots\}$

Q33. If P is the solution set of $-3x+4 < 2x-3$, $x \in N$ and Q is the solution set of $4x-5 \leq 12$, $x \in W$, find (i) $P \cap Q$ (ii) $Q - P$

Sol.

$$\begin{aligned} -3x+4 &< 2x-3 & 4x-5 &\leq 12 \\ -5x &< -7 & 4x &\leq 17 \\ x &> \frac{7}{5} & x &\leq \frac{17}{4} \\ P = \{2, 3, 4, \dots\} & & Q = \{0, 1, 2, 3\} \\ (i) P \cap Q = \{2, 3\} & (ii) Q - P = \{0, 1\} \end{aligned}$$

Q34. $A = \{x : 11x-5 > 7x+3, x \in R\}$ and $B = \{x : 18x-9 \geq 15 + 12x, x \in R\}$. find the range of set $A \cap B$ and represent it on a number line.

Sol.

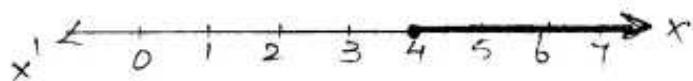
$$\begin{aligned} A &= 11x-5 > 7x+3 & B &= 18x-9 \geq 15 + 12x \\ 4x &> 8 & 18x &\geq 24 \\ x &> 2 & 6x &\geq 24 \\ & & x &\geq 4 \end{aligned}$$

$\therefore A \cap B$
 $A = \{3, 4, 5, 6, \dots\}$ $B = \{4, 5, 6, 7, \dots\}$

$$\therefore A \cap B = \{4, 5, 6, \dots\}$$

$$\Rightarrow A \cap B = \{x : x \in R, x \geq 4\}$$

solution set on number Line



Q35. Given $P = \{x : x \in R, 5 < 2x - 1 \leq 11\}$

$Q = \{x : x \in I, -1 \leq 3 + 4x < 23\}$ where
R = Real numbers, I = Integers. Represent
P and Q on number Lines. Write down the
elements of $P \cap Q$.

sol. $P = 5 < 2x - 1 \leq 11$

$$5 < 2x - 1 \quad \text{and} \quad 2x - 1 \leq 11$$

$$-2x < -6 \quad \text{and} \quad 2x \leq 12$$

$$x > 3 \quad \text{and} \quad x \leq 6$$

solution set $3 < x \leq 6 = \{4, 5, 6\}$

solution set on number line:



$Q = -1 \leq 3 + 4x < 23$

$$-1 \leq 3 + 4x \quad \text{and} \quad 3 + 4x < 23$$

$$-4x \leq 4 \quad \text{and} \quad 4x < 20$$

$$x \geq -1 \quad \text{and} \quad x < 5$$

$$-1 \leq x, \quad -1 \leq x < 5$$

solution set $= \{-1, 0, 1, 2, 3, 4\}$

solution set on number line



$$\therefore P \cap Q = \{4\}$$

- Q36. If $x \in \mathbb{I}$, find the smallest value of x which satisfies the inequation $2x + \frac{5}{2} > \frac{5x}{3} + 2$.

Sol.

$$\begin{aligned}2x + \frac{5}{2} &> \frac{5x}{3} + 2 \\ \Rightarrow 2x - \frac{5x}{3} &> 2 - \frac{5}{2} \\ \Rightarrow 12x - 10x &> 12 - 15 \\ \Rightarrow 2x &> -3 \\ \Rightarrow x &> -\frac{3}{2}\end{aligned}$$

\therefore smallest value of $x = -1 \quad \{ \because x \in \mathbb{I} \}$

- Q37. Given $20 - 5x < 5(x+8)$, find the smallest value of x , when (i) $x \in \mathbb{I}$, (ii) $x \in \mathbb{W}$, (iii) $x \in \mathbb{N}$.

Sol.

$$\begin{aligned}20 - 5x &< 5(x+8) \\ \Rightarrow 20 - 5x &< 5x + 40 \\ \Rightarrow -10x &< 20 \\ \Rightarrow x &< 2 \\ \Rightarrow x &> -2\end{aligned}$$

(i) when $x \in \mathbb{I}$, then smallest value = -1

(ii) when $x \in \mathbb{W}$, then smallest value = 0

(iii) when $x \in \mathbb{N}$, then smallest value = 1

- Q38. solve the given inequation and graph the solution on the number line : $2y - 3 < y + 1 \leq 4y + 7$; $y \in \mathbb{R}$

$$2y - 3 < y + 1 \leq 4y + 7$$

$$2y - 3 < y + 1 \quad \text{and} \quad y + 1 \leq 4y + 7$$

$$y < 4 \quad \text{and} \quad -3y \leq 6$$

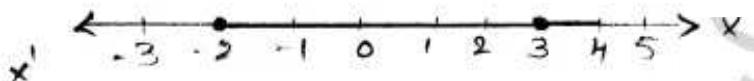
$$-y \leq 2$$

$$y \geq -2$$

$$\therefore -2 \leq y \leq 4$$

\therefore The solution set = { $y : y \in \mathbb{R}, -2 \leq y \leq 4$ }

solution set on Number Line



- Q39. find the greatest integer which is such that if 7 are added to its double, the resulting number becomes greater than three times the integer.

sol. let the integer be x

Now, according to the question

$$2x + 7 > 3x$$

$$\Rightarrow -x > -7$$

$$\Rightarrow x < 7$$

\therefore The greatest integer will be 6 which is less than 7.

- Q40. one-third of a bamboo pole buried in mud, one-sixth of it is in water and part above the water is greater than or equal to 3 meters. find the length of the shortest pole.

sol. let the length of the pole be x m.

Now according to the question

$$\frac{1}{3}x + \frac{1}{6}x = \text{part buried in mud} + \text{part in water}$$

$$\Rightarrow \frac{3}{6}x = \frac{x}{2} = \text{half part of pole is in mud \& water}$$

Now according to the question remaining part ie, half above the water is greater than or equal to 3 meters.

$$\Rightarrow \frac{x}{2} \geq 3$$

$$\Rightarrow x \geq 6$$

∴ the length of the shortest pole is 6 meters.