

Sets

Exercise - 5.1

Solution - 01 :-

(i) It is a set

If we denote the given set by A, then

$$A = \{1, 3, 5, 7, 9, 11, 13, 15, 17, \dots, \dots, 43, 45, 47, 49\}$$

(ii) It is not a set because the given collection is not well-defined - colors may differ when we choose four among seven.

(iii) It is a set

If we denote the given set by A, then $A = \{\text{Sun, Mon, Tue}\}$

(iv) It is not a set because the given collection is not well defined - people may differ on whether a student tall or not

(v) It is not a set because the given collection is not well defined - people may differ on whether clever may vary in the school.

(vi) It is not a set because the given collection is not well defined - people may differ on whether rich people in Bengaluru among population or not

(vii) It is not a set because the given collection is not well defined - multiples of 5 may vary in each set.

(viii) collection of all prime numbers.

It is a set.

If we denote the given set by A, then $A = \{2, 3, 5, 7, 11, 13, 17, 19, \dots\}$.

(ix) It is a set

If we denote the given set by A, then

$$A = \{-4, -2, 2, 4, 6, 8, 10, 12, 14\}.$$

(x) It is not a set because people may differ on whether a cricket player is good or not

(xi) It is a set.

If we denote the given set by A, then

$$A = \{x, y, z\}.$$

(xii) It is not a set because people may differ on whether a student of school among the three is healthy students or not.

Solution-02:-

(i) \in

(ii) \in

(iii) \notin

(iv) \notin

(v) \notin

(vi) \in

Solution - 03 :-

(i) False

(ii) False

(iii) True

(iv) False

(v) True

(vi) False

Solution - 04 :-

(i) The given set can be written as

$$\{1, 3, 5, 7, 9\}$$

(ii) The given set can be written as

$$\{2, 4, 6, 8, \dots, 100\}$$

(iii) The given set can be written as

$$\{\text{April, August, October}\}$$

(iv) The given set can be written as

$$\{1, 4, 9\}$$

(v) The given set can be written as

$$\{-14, -7, 0, 7, 14, 21\}$$

(vi) The given set can be written as

$$\{1, 2, 3, 4, 6, 9, 12, 18, 36\}$$

(vii) The given set can be written as

$$\{2, 3, 5\}$$

(viii) The given set can be written as

$$\{0, 5, 10, 15, \dots\}$$

(ix) The given set can be written as

$$\{C, H, E, N, A, I\}$$

(x) The given set can be written as

$$\{U, O, I, E\}$$

(xi) The given set can be written as

$$\{M, T, H, C, S\}$$

Solution-05:-

The given set can be written as

(i) $\{1, 2, 3, 4, 5, 6\}$

{ Natural numbers less than 7 }

(ii) $\{0, 1, 2, 3, 4, 5\}$

{ Whole numbers less than or equal to 5 }

(iii) $\{\text{February, April, June, September, November}\}$

{ Months which are having less than 31 days }

(iv) $\{C, I, R, C, O, M, F, E, N\}$

{ Letters in the word CIRCUMFERENCE }

(v) $\{O, A, I\}$

{ Vowels in the word NOTATION }

(vi) $\{1, 0, 5, 2, 6, 7\}$

{ digit in the numeral 110526715 }

(vii) $\{1, 2, 3, 4, 6, 8, 12, 16, 24, 48\}$

{ x is a factor of 48 }

(viii) $\{0, 11, 22, 33, 44, 55, 66, 77\}$

{ Numbers are multiples of 11 b/w 0 & 80 }

(ix). $\{10, 20, 30, 40, \dots, 90\}$

{ two digit natural numbers which is divisible by 10 }

Solution-06:-

The set can be written as.

(i) $\{-2, -1, 0, 1, 2, 3\}$ Roster form

$\{x : x \in \mathbb{Z}, -2 \leq x \leq 3\}$ Set Builder form.

(ii) $\{U, L, T, I, M, A\}$ Roster form

$\{x : x \text{ is a letter in the word 'ULTIMATUM'}$
Set Builder form

(iii) $\{\text{January, June, July}\}$ Roster form

$\{x | x \text{ is a month of a year whose name begins with J}\}$. S.B form

(iv) $\{0, 1, 4, 9\}$ Roster form

$\{x | x \text{ is a perfect square 1 digit number}\}$
Set Builder form.

Solution-07:-

The given set can be written as.

(i) $\{2, 3, 5, 7, 11, 13, 17, 19, 23, 29\}$ Roster form

$\{\text{Prime numbers less than } 30\}$ Descriptive form.

(ii) $\{0, 8, 16, 24, 32, 40, 48\}$ Roster form

$\{\text{whole numbers which are multiples of 8 and less than } 50\}$.

(iii) $\{\Theta, S, T, N, P, R\}$; Roster form

{constants in the word 'QUESTION PAPER'}

Set Builder form

Solution - 08 :-

(i) Here, the members of A are whole numbers
are lying less than or equal to 11.

$$A = \{x : x \in W, x \leq 11\}$$

(ii) $B = \{x : x = 7n, n \in N\}$
Multiples of 7 & Natural numbers

(iii) $C = \{x : x = n^2, n \in N \text{ and } n \leq 7\}$

(iv) $D = \{x : x = 3n, n \in I \text{ and } -4 \leq n \leq 6\}$.

Exercise - 5.2

Solution :-

- (i) Given $A = \{ \text{all colors of rainbow} \}$
= $\{ V, I, B, G, Y, O, R \}$ which has seven elements

$$n(A) = 7.$$

It is a finite set

- (ii) Given $A = \{ x | x \text{ is a prime number, b/w } 7 \text{ & } 11 \}$
= $\{ \}$

Empty set

- (iii) $\{ \text{multiples of } 5 \}$

$$\{ 5, 10, 15, \dots \}$$

Infinite set

- (iv) $\{ \text{all straight lines can be drawn in a plane} \}$
 $\{ l, m, n, \dots \}$

Infinite set

- (v) $\{ x | x \text{ is a digit in the numeral } 550131527 \}$

$$\{ 5, 0, 1, 3, 2, 7 \}$$

finite set, \emptyset

$$n(A) = 6$$

(vi) $\{x : x \text{ is a letter in the word 'SUFFICIENT'}\}$

$$\{ S, U, F, I, C, E, N, T \}$$

finite set

$$n(A) = 8.$$

(vii) $\{x : x \text{ is a vowel in the word MATHEMATICS}\}$

$$\{ A, E, I \}$$

finite set

$$n(A) = 3$$

(viii) $\{x : x \text{ is an even whole number and } x \leq 20\}$

$$\{0, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20\}$$

finite set

$$n(A) = 11.$$

(ix) $\{x : x \in \mathbb{Z} \text{ and } -2 \leq x \leq 5\}$

$$\{-2, -1, 0, 1, 2, 3, 4\}$$

finite set

$$n(A) = 7.$$

(x) $\{x : x \text{ is a prime number less than } 25\}$

$$\{2, 3, 5, 7, 11, 13, 17, 19, 23\}$$

finite set

$$n(A) = 9.$$

(xi) $\{x : x \text{ is a prime factor of } 180\}$

$$\{2, 3, 5\}, n(A) = 3.$$

(xii) $\{x : x \in \mathbb{N} \text{ and } x \text{ is a composite number} < 12\}$

$$\{4, 6, 8, 9, 10, 12\}$$

finite set, 5

Solution - 02

(i) $A = \{2, 4, 6, 8, 10\}$

$B = \{\text{even natural numbers}\}$

$$= \{8, 10, 12, 14, 16\}$$

$$A \neq B$$

(ii) $A = \{3, 5, 7, 9, 11, 13\}$

$B = \{\text{odd natural numbers between 2 and 14}\}$

$$B = \{3, 5, 7, 9, 11, 13\}$$

$$A = B$$

(iii) $A = \{\text{PUPPETY}\}$ $B = \{P, U, E, T\}$

$$A \neq B$$

(iv) $A = \{x | x \text{ is a letter in the word SOPHIA}\}$

$B = \{x | x \text{ is a letter in the word MUMTAZ}\}$

$$A = \{S, O, P, H, I, A\}$$

$$B = \{M, U, T, A, Z\}$$

$$A \neq B$$

(V) $A = \{ \text{kids 5 meters tall} \}$

$B = \{x; x \in \mathbb{N} \text{ and } 2x = 3\}$

$A = B$.

Solution-03.

Given that

$$A = \{2, 5, 7, 8, 10\}$$

$$B = \{5, 7, 2, x, 10\}$$

$$B = \{2, 5, 7, x, 10\}$$

$$A = B$$

then

$$\boxed{x = 8}$$

the numerator and denominator of the first fraction by 5.

$$\text{So } \frac{2}{3} = \frac{2 \times 5}{3 \times 5} \\ = \frac{10}{15}.$$

(ii) $\frac{7}{18} = \frac{42}{\square}$

The denominator in the first fraction is 18.

Numerator in the first fraction is 7.

∴ To make both fractions equal, we multiply the numerator and denominator of the first fraction by 6.

$$\frac{7}{18} = \frac{7 \times 6}{18 \times 6} = \frac{42}{108}$$

(iii) $\frac{4}{\square} = \frac{12}{15}$.

The numerator in the second fraction is 12.

∴ To make both fractions equal, we multiply the numerator and denominator of the first fraction by $\frac{1}{3}$.

$$\boxed{\frac{4}{\square}} = 4x$$

$$\frac{12}{15} = \frac{12 \times \frac{1}{3}}{15 \times \frac{1}{3}}$$

$$\Rightarrow \frac{4}{5} = \frac{12}{15}.$$